

Spectroscopic Identification of Organic Molecules

¹H NMR Spectroscopy

Exclusively for the summer course at
East China University of Science and Technology

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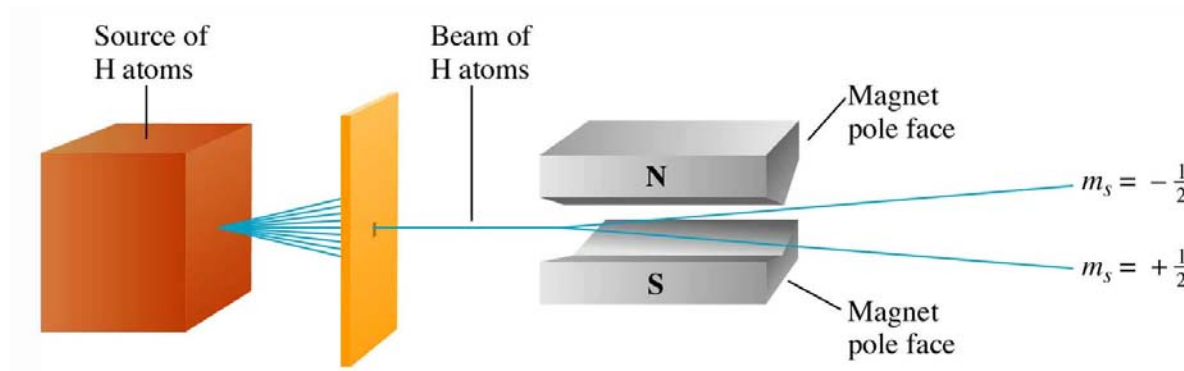
Not for sale or distribution but only for the class

¹H NMR Spectroscopy

1. Basic Theory of NMR

1.1 Magnetic Properties of Nuclei

Experiment by Stern-Gerlach: A beam of H-atoms splits into two by a magnetic field.



Spin angular momentum (\underline{P}):

$$\underline{P} = \underline{I} \cdot \hbar \quad (\hbar = h/2\pi)$$

I : spin quantum number,

$$|\underline{I}| = [I \cdot (I+1)]^{1/2}$$

Magnetic moment ($\underline{\mu}$):

$$\underline{\mu} = \gamma \cdot \underline{P}$$

γ : gyromagnetic ratio

$$\gamma = \underline{\mu} / \underline{P} = \mu / [I \cdot (I+1)]^{1/2} \cdot \hbar$$

= magnetic moment / angular momentum

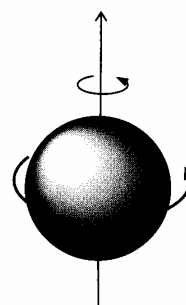


FIGURE 3.1 Spinning charge on proton generates magnetic dipole.

TABLE 3.1 Type of nuclear spin number, I , with various combinations of atomic mass and atomic number.

I	Atomic Mass	Atomic Number	Example of Nuclei
Half-integer	Odd	Odd	${}^1_1\text{H}(\frac{1}{2})$, ${}^3_1\text{H}(\frac{1}{2})$, ${}^{15}_7\text{N}(\frac{1}{2})$, ${}^{19}_9\text{F}(\frac{1}{2})$, ${}^{31}_{15}\text{P}(\frac{1}{2})$
Half-integer	Odd	Even	${}^{13}_6\text{C}(\frac{1}{2})$, ${}^{17}_8\text{O}(\frac{1}{2})$, ${}^{29}_{14}\text{Si}(\frac{1}{2})$
Integer	Even	Odd	${}^2_1\text{H}(1)$, ${}^{14}_7\text{N}(1)$, ${}^{10}_5\text{B}(3)$
Zero	Even	Even	${}^{12}_6\text{C}(0)$, ${}^{16}_8\text{O}(0)$, ${}^{34}_{16}\text{S}(0)$

1.2 Spinning Nuclei in a Magnetic Field

A spinning nucleus ($I = 1/2$) in a uniform magnetic field (B_0):

Precessional motions along side (α , $+1/2$) and the opposite side (β , $-1/2$) to the applied magnetic field. Precessional angle $\rightarrow 54.5^\circ$.

Precessional frequency (ω): Larmor frequency,

$$\omega = (1/2\pi) \cdot \gamma \cdot B_0 = \{ \mu / (I \cdot \hbar) \} \cdot B_0 \quad \therefore \gamma = \mu / p = \mu / (I \cdot \hbar) = 2\pi\mu / (I \cdot \hbar)$$

$$\text{Zeeman Level } (\Delta E) = 2\mu \cdot B_0$$

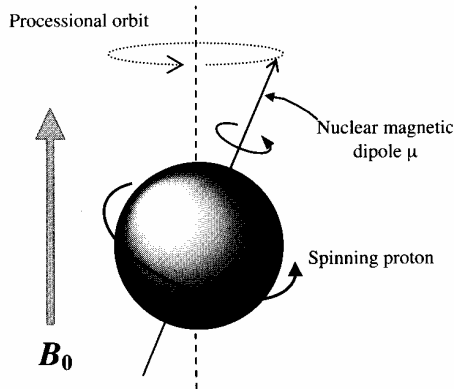


FIGURE 3.3 Classical representation of a proton precessing in a magnetic field of magnitude B_0 in analogy with a precessing spinning top.

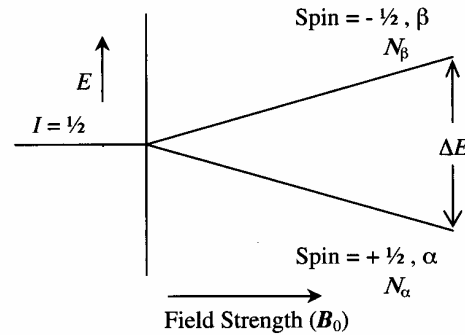


FIGURE 3.2 Two proton energy levels in a magnetic field of magnitude B_0 . N is population of spins in the upper (N_β) and lower (N_α) energy states. The direction of the magnetic field (B_0) is up, parallel to the ordinate, and field strength (B_0) increases to the right. Larger (B_0) fields increase ΔE .

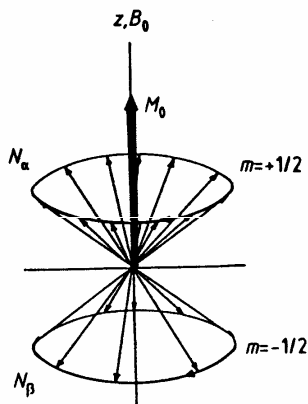
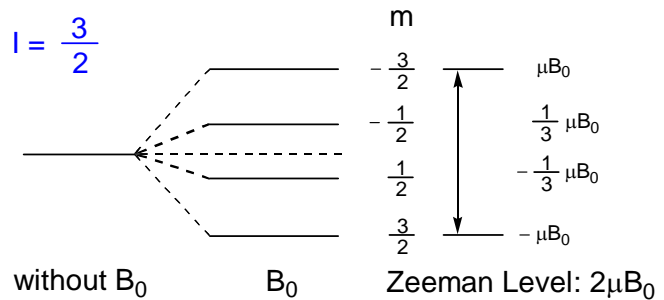


Figure 1-5. Distribution of the precessing nuclear dipoles (total number $N (= N_\alpha + N_\beta)$) around the double cone. As $N_\alpha > N_\beta$ there is a resultant macroscopic magnetization M_0 .

In general, nuclear spin I can have $2I + 1$ energy levels ($I, I-1, I-2, \dots, -I$), and each level is separated by $(\mu/I) \cdot B_0$.



Example)

$B_0 = 1.41$ T (60 MHz) at 300 K (27 °C),

$\Delta E \approx 2.4 \times 10^{-2}$ J/mole

$N_\beta \approx 0.9999904 N_\alpha$

For 300 MHz,

$N_\beta \approx 0.99995 N_\alpha$

$$\frac{N_\beta}{N_\alpha} = e^{-\Delta E/k_B T} \approx 1 - \frac{\Delta E}{k_B T} = 1 - \frac{\gamma \hbar B_0}{k_B T} \quad (1-10)$$

where k_B is the Boltzmann constant ($= 1.3805 \times 10^{-23}$ J K $^{-1}$) and T is the absolute temperature in K.

1.3 NMR Experiment

Alternating magnetic field B_1 , which is perpendicular to B_0 is applied to the sample to induce the transition between the Zeeman levels.

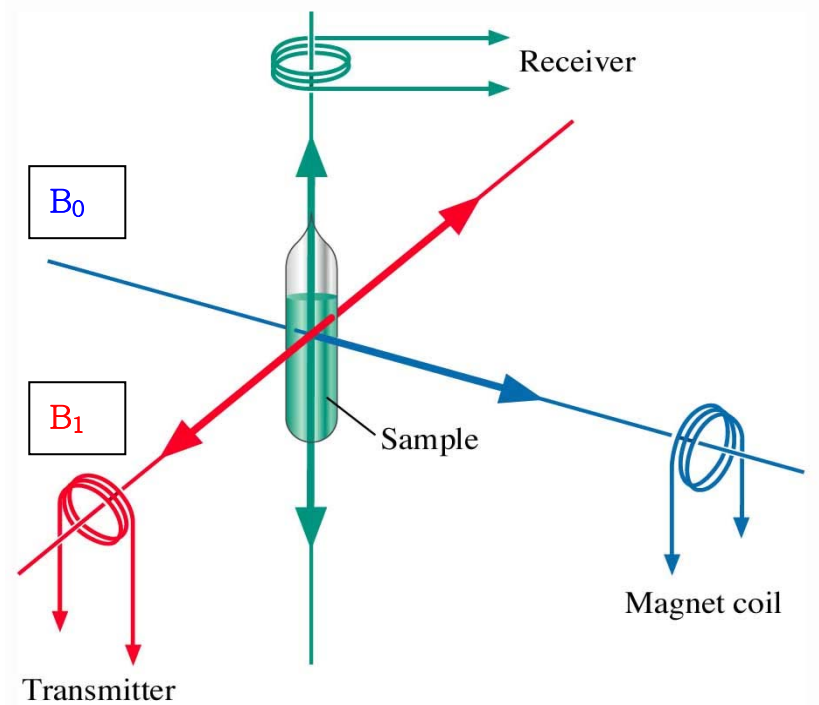
$\Delta E = h\nu = (\mu/I) \cdot B_0$, allowed transition: $\Delta m = \pm 1$.

ν of B_1 :

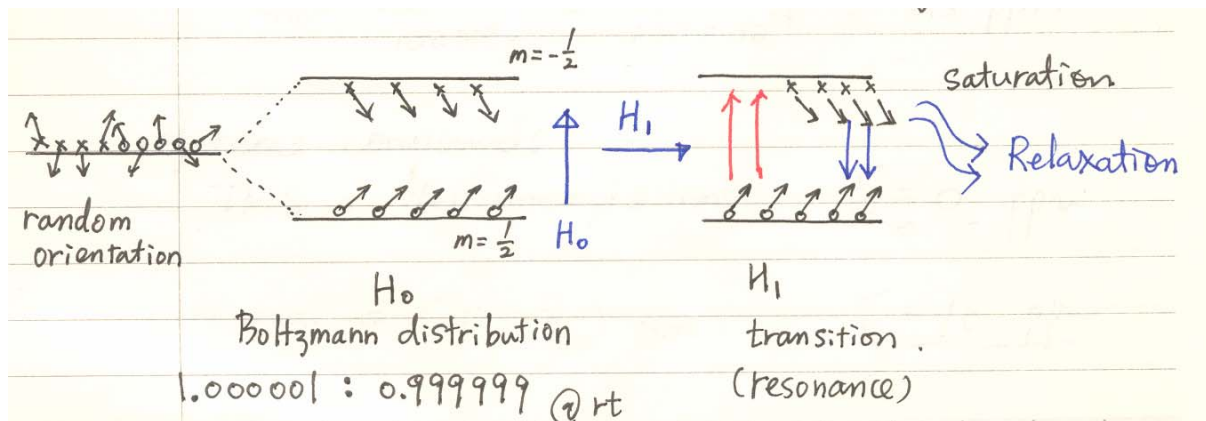
$B_0 = 9,395$ gauss
then, ν of $B_1 = 40$ MHz

$B_0 = 14,095$ gauss
then, ν of $B_1 = 60$ MHz

$B_0 = 23,490$ gauss
then, ν of $B_1 = 100$ MHz



Relaxation:



Spin-lattice relaxation:

Photon without radiation, giving energy to the vibrational system.

Photon with radiation (minor effect)

Relaxation time: T_1

Spin-Spin relaxation time:

Spin exchange

Relaxation time: T_2

$$\mathbf{B_{effective} = B_0 - \alpha \cdot B_0 = B_0 \cdot (1 - \alpha)}$$

α : diamagnetic shielding constant – reflects chemical and magnetic environments of the nuclei.

α : 10^{-5} (proton) $\sim 10^{-2}$, if $B_0 = 15$ Kgauss (~ 60 MHz), then $B_0 \cdot \alpha = 0.15$ gauss = ~ 600 Hz.

2. Chemical Shift δ (ppm): Dimensionless parameter, independent of B_0

Chemical shifts have their origin in **diamagnetic and paramagnetic shielding effects** produced by circulation of both bonding and non-bonding electrons in the neighborhood of the nuclei.

$$\delta_{AB} = (v_A - v_B) / B_0$$

Example)

B_0 : 300 MHz, $v_A - v_B = 150$ Hz

$$\delta_{AB} = 150 \text{ Hz} / 300 \text{ MHz} = 150 \text{ Hz} / 300 \times 10^6 \text{ Hz} = 0.5 \text{ ppm}$$

B_0 : 600 MHz, $v_A - v_B = 300$ Hz

$$\delta_{AB} = 300 \text{ Hz} / 600 \text{ MHz} = 300 \text{ Hz} / 600 \times 10^6 \text{ Hz} = 0.5 \text{ ppm}$$

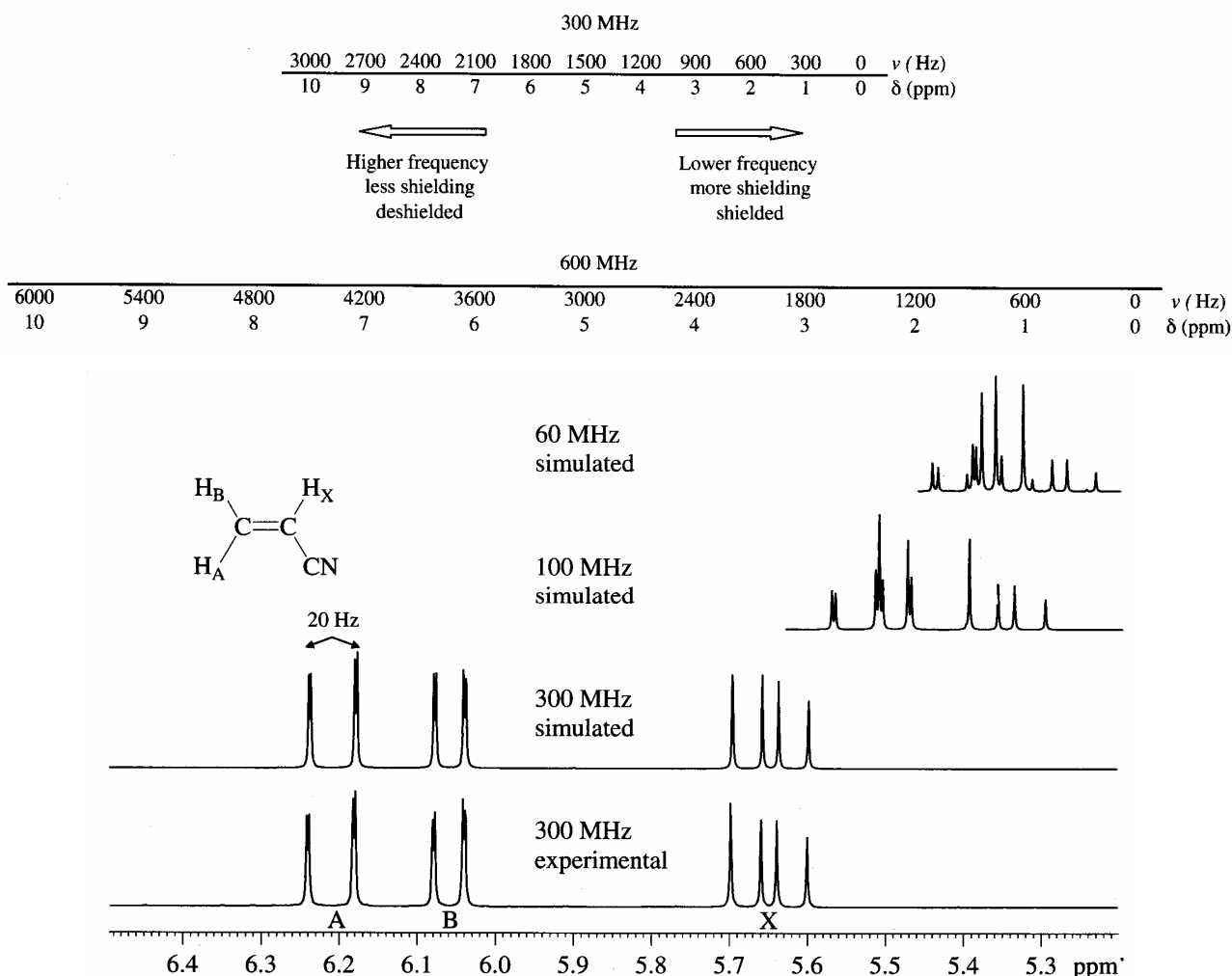
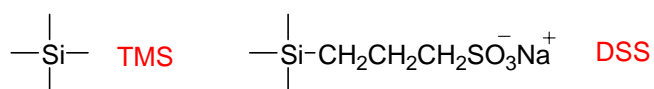


FIGURE 3.19 Simulated 60, 100, and 300 MHz ^1H spectra of acrylonitrile; 300 MHz experimental spectrum (in CDCl_3) for comparison.

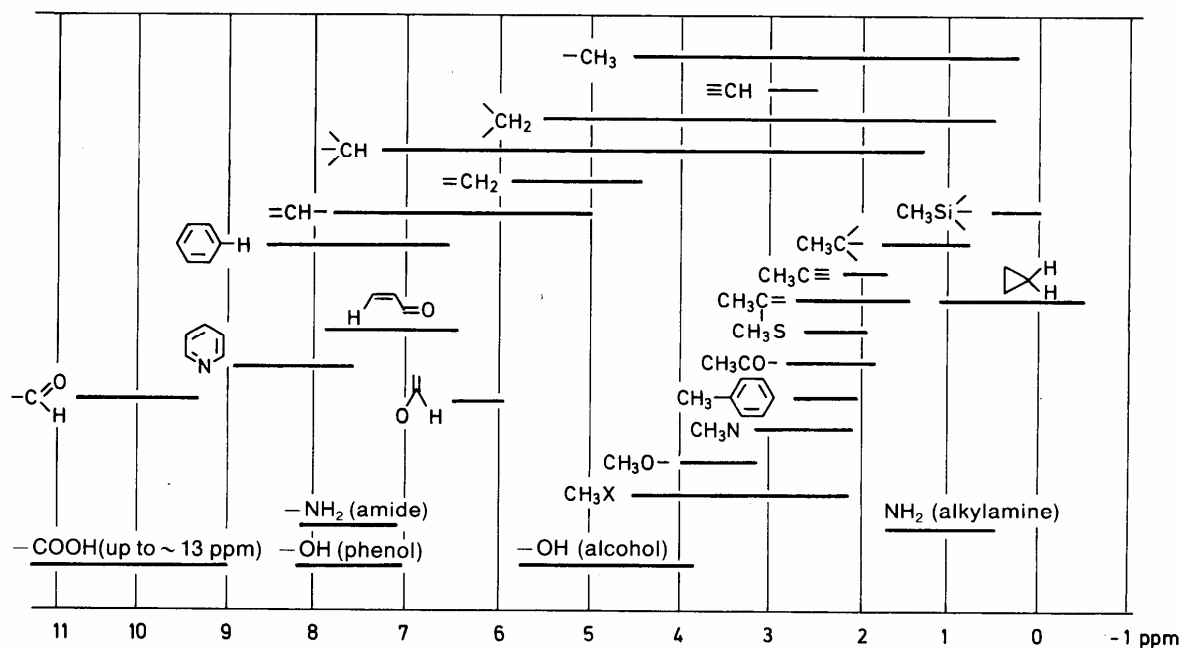
Reference compound $\delta = 0$ ppm.

(1) TMS (tetramethylsilane)

(2) DSS (sodium 2,2-dimethyl-2-silapentane-5-sulfonate)



Chemical shifts referred to DSS or TMS agree within ~ 0.02 ppm. The sharp singlet is not influenced by pH changes. The multiplet of CH_2 in DSS are not significant at concentrations $< 1\%$.



► Empirical Additive Rules

(1) Dailey, Shoolery's Rule

(*J. Am. Chem. Soc.* **1955**, 77, 3977)



$\tau = 9.77 - \sum S(\delta)$ $\delta = 10 - \tau$

$\delta = 0.23 + \sum S(\delta)$

(2) Electronegativity of X



$\text{E.N. (X)} = 0.684 \cdot (\delta_{\text{CH}_2} - \delta_{\text{CH}_3}) + 1.78$

Table 4.3 Substituent constants, $S(\delta)$, for proton resonances in substituted methanes

Substituent	$S(\delta)$ (ppm)
Cl	2.53
Br	2.33
I	1.82
NRR'	1.57
OR	2.36
SR	1.64
CR—O	1.70
CR=CR'R'	1.32
C≡CH	1.44
C≡N	1.70
CH ₃	0.47
Phenyl	1.85
OH	2.56
OCOR	3.13
COOR	1.55
CF ₃	1.14

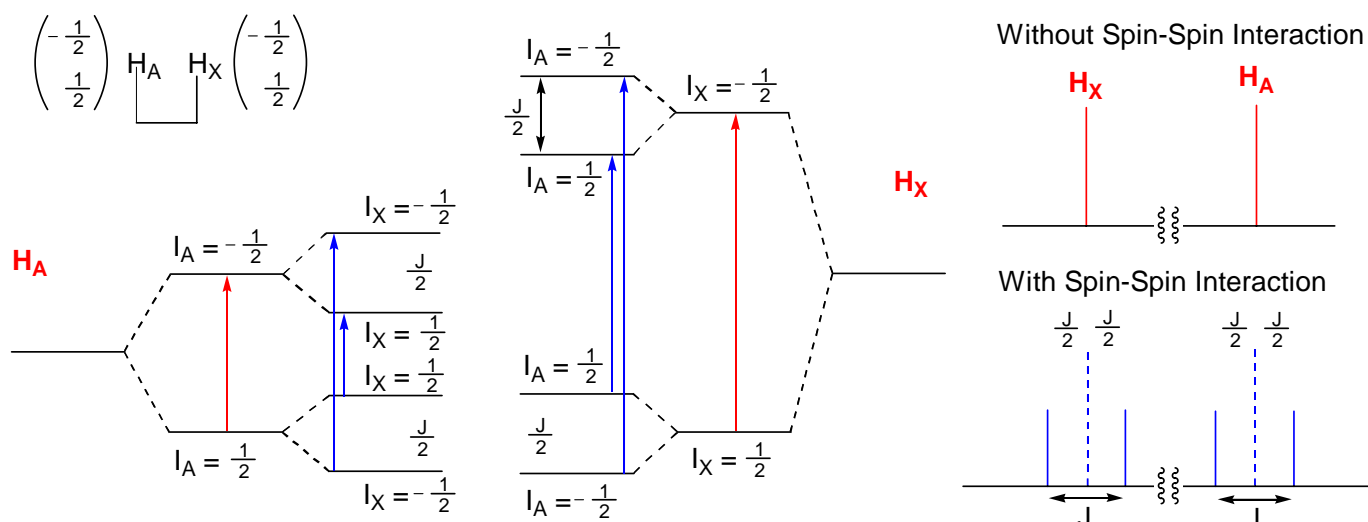
3. Spin-Spin Coupling Constants (J)

Nuclei changes the local magnetic field (effective magnetic filed) of each nucleus by **attractive or repulsive interaction of each magnetic quantum number**. Since nuclear magnetic moments are **independent of the applied field B_0** , so is the coupling constant J.

AX system: $\delta_{AB} \cdot B_0 / J \geq 10$

Since $\delta_{AX} = (v_A - v_B) / B_0$, then $(v_A - v_B) / J \geq 10$

AX System



H_A-C-CH_2 and H_A-C-CH_3

CH ₂ group	m_T	CH ₃ group	m_T
$\alpha\alpha$	+1	$\alpha\alpha\alpha$	$+\frac{3}{2}$
$\alpha\beta \quad \beta\alpha$	0	$\alpha\alpha\beta \quad \alpha\beta\alpha \quad \beta\alpha\alpha$	$+\frac{1}{2}$
$\beta\beta$	-1	$\alpha\beta\beta \quad \beta\alpha\beta \quad \beta\beta\alpha$	$-\frac{1}{2}$
		$\beta\beta\beta$	$-\frac{3}{2}$

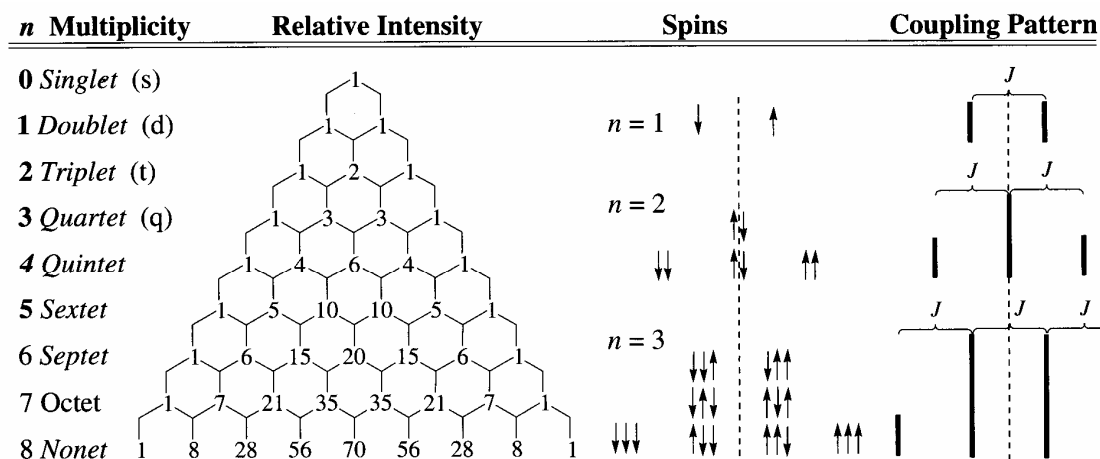
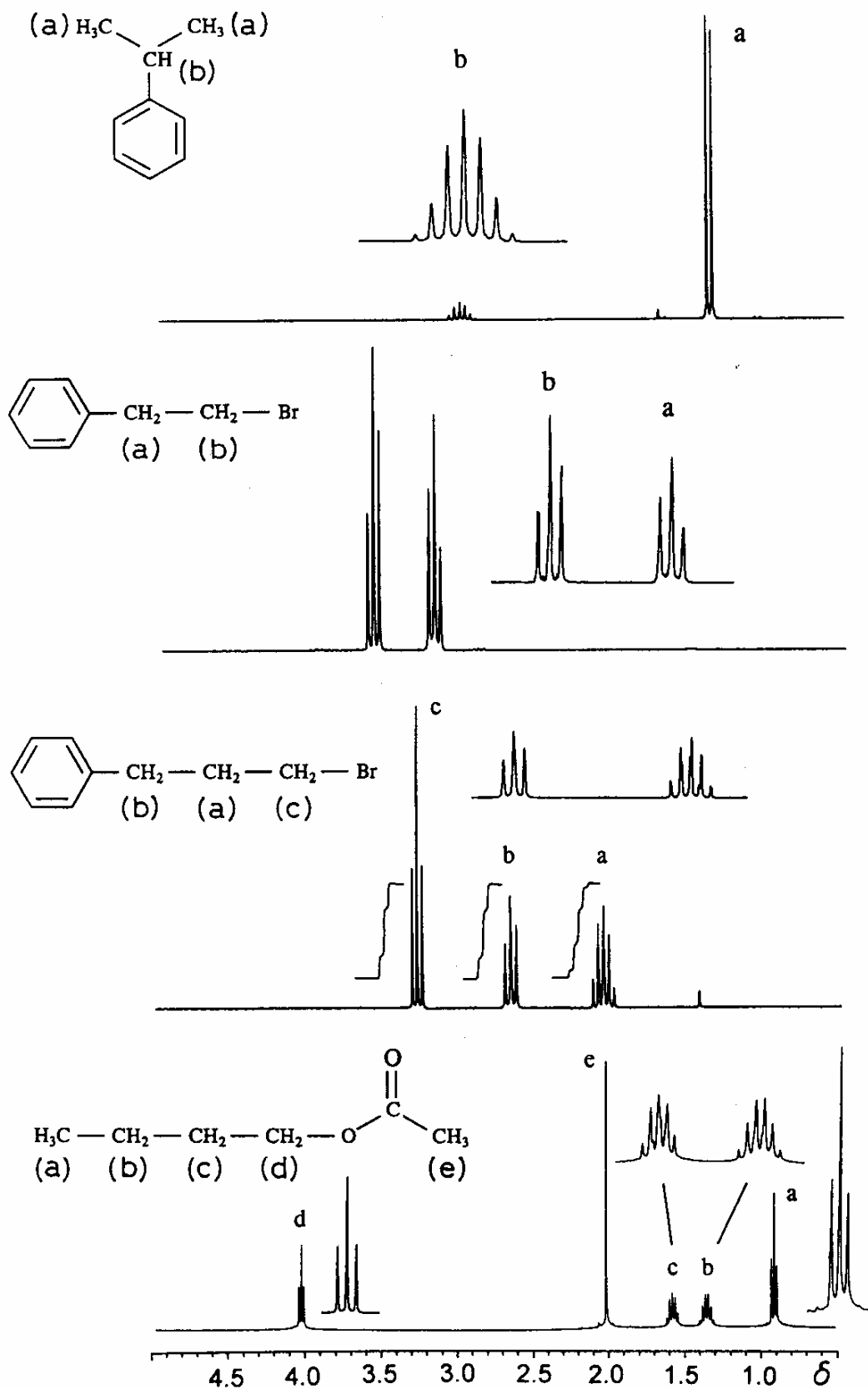


FIGURE 3.32 Pascal's triangle. Relative intensities of first-order multiplets; n = number of equivalent coupling nuclei of spin 1/2 (e.g., protons).

Characteristic splitting patterns in the ^1H NMR spectra of some alkyl groups.



3-1. Vicinal H-H Couplings (${}^3J_{HH}$)

(1) The couplings in both saturated and unsaturated systems are largely transmitted via the σ -electrons, and these are always positive.

In general, ${}^3J(\text{sp}^2\text{-sp}^2) > {}^3J(\text{sp-sp}) > {}^3J(\text{sp}^3\text{-sp}^3)$
25 ~ 7 Hz 9.1 Hz 12 ~ 2 Hz

(2) Dihedral angle dependency

Karplus (1963): $J = 4.22 - 0.5 \cdot \cos\phi + 4.5 \cdot \cos^2\phi$

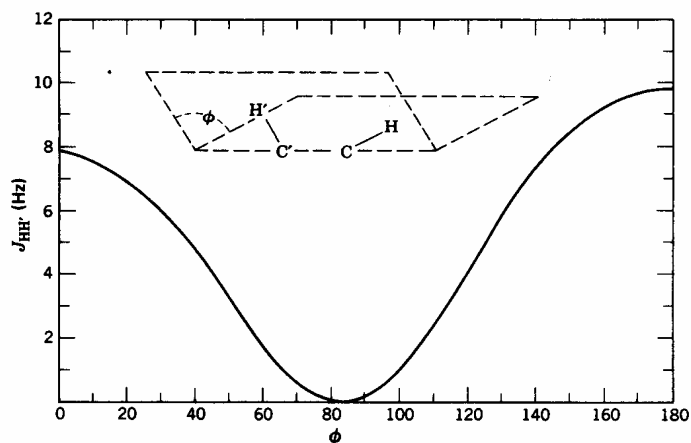


FIGURE 3.57 The vicinal Karplus correlation. Relationship between dihedral angle (ϕ) and coupling constant for vicinal protons.

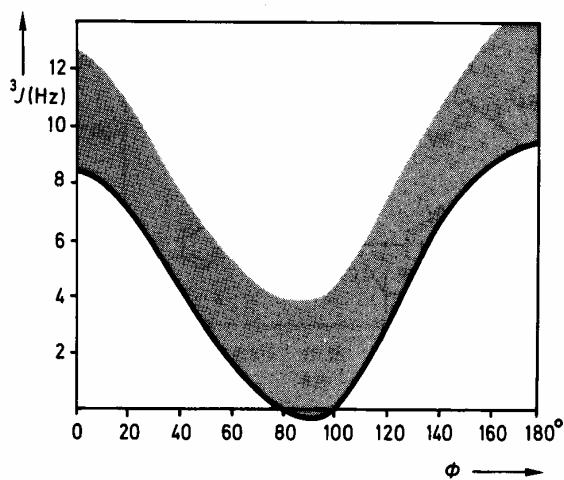


Figure 4.22 The Karplus curve for the dependence of vicinal H-H coupling on the dihedral angle ϕ : line, theoretical curve; shaded area, range of empirical results

A. Six-membered Ring Systems (all sp^3 carbons)

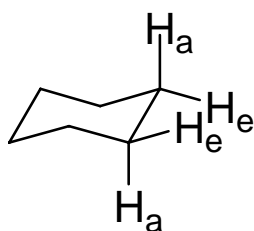
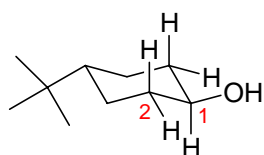


TABLE 3.6. Calculated and observed coupling constants, J , in cyclohexanes based on bond angle.

	Dihedral Angle	Calculated J (Hz)	Observed J (Hz)
Axial-axial	180°	9	8–14 (usually 8–10)
Axial-equatorial	60°	1.8	1–7 (usually 2–3)
Equatorial-equatorial	60°	1.8	1–7 (usually 2–3)

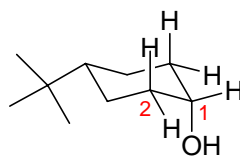
Examples

①



$$J_{H1,H2eq} = +4.31$$

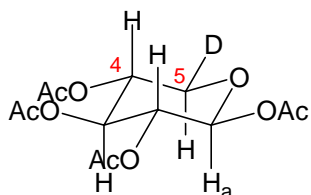
$$J_{H1,H2ax} = +11.07$$



$$J_{H1,H2eq} = +2.72$$

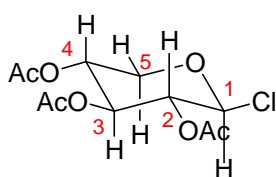
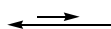
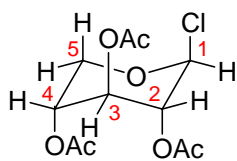
$$J_{H1,H2ax} = +3.00$$

② The value of J is reduced by an electron withdrawing group



$$J_{4,5} = +8.1 \text{ Hz}$$

③ Anomeric effect

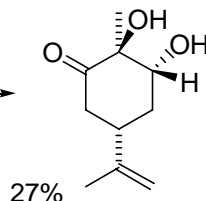
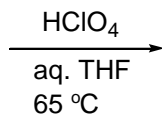
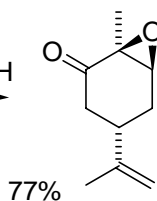
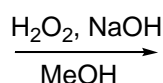
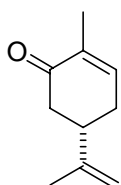


$$J_{1,2} = 2.0 \text{ Hz}, J_{1,3} = 1.5 \text{ Hz}$$

$$J_{3,5e} = 0.6 \text{ Hz}, J_{4,5a} = 3.0 \text{ Hz}$$

$$J_{4,5e} = 3.7 \text{ Hz}, J_{5a,5e} = 12.9 \text{ Hz}$$

④

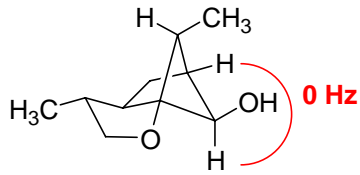
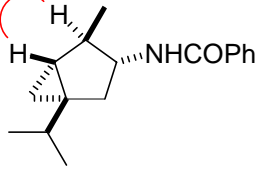


$$3.77 \text{ (dd, } J = 5, 11 \text{ Hz)}$$

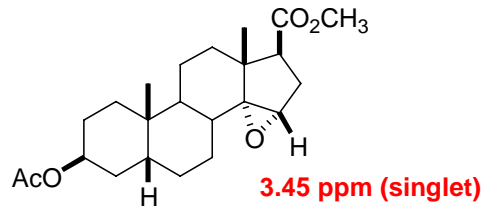
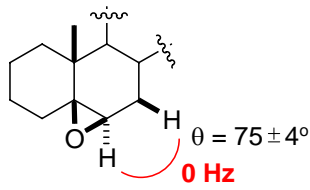
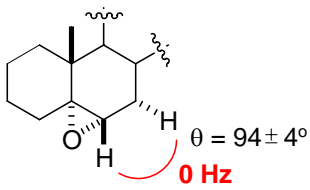
⑤ Small 3J

a. dihedral angle $\sim 90^\circ$

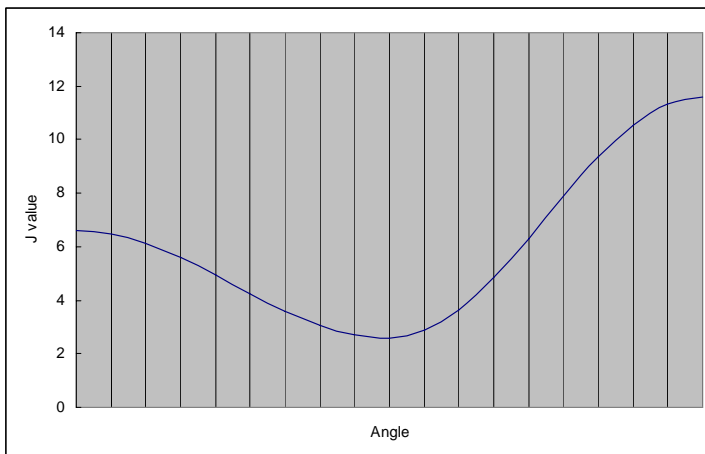
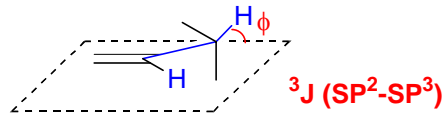
0 Hz



b. epoxide H's



B. 3J (sp^2-sp^3)



$$0^\circ \leq \theta \leq 90^\circ$$

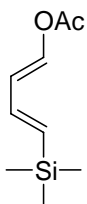
$$J = 6.6 \cdot \cos^2\theta + 2.6 \cdot \sin^2\theta$$

$$90^\circ \leq \theta \leq 180^\circ$$

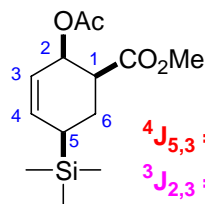
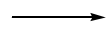
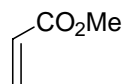
$$J = 11.6 \cdot \cos^2\theta + 2.6 \cdot \sin^2\theta$$

$$6.6 (0^\circ), 2.7 (90^\circ), 11.7 (180^\circ)$$

Examples



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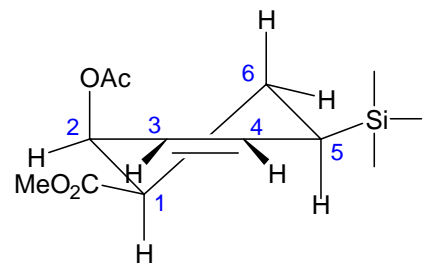


$$^4J_{5,3} = 2.7 \text{ Hz}, \quad ^3J_{5,4} = 1.2 \text{ Hz},$$

$$^3J_{2,3} = 5.6 \text{ Hz}, \quad ^3J_{3,4} = 10.2 \text{ Hz},$$

$$^3J_{1,2} = 3.4 \text{ Hz}, \quad ^3J_{1,6e} = 3.4 \text{ Hz},$$

$$^3J_{1,6a} = 13.1 \text{ Hz}$$



C. Amino Acid Derivatives

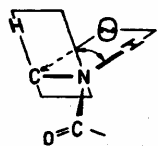
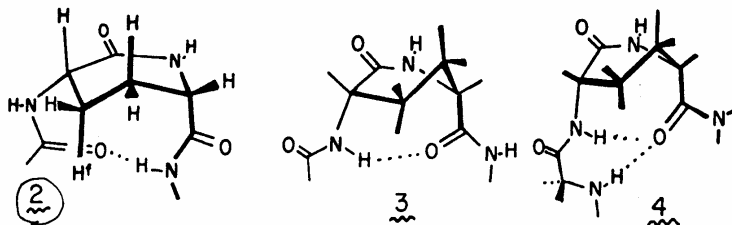
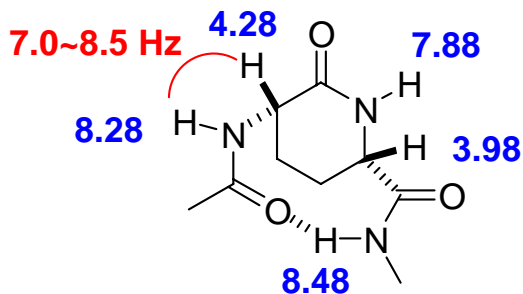
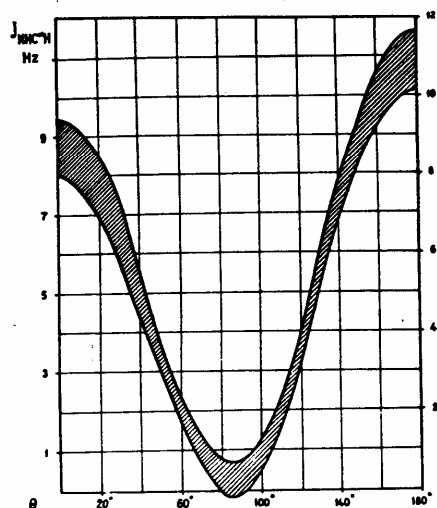


Fig. 4. Dihedral angle θ between the H-N-C' and N-C'-H planes.



(3) CH-CH-X: Increasing electro-negativity of X gives smaller 3J

$$^3J = J_0 - \alpha \cdot Ex \quad Ex: \text{electronegativity of X}; \quad J_0, \alpha: \text{constants}$$

	J	J_0 (Hz)	α (Hz)
CH ₃ -CH ₂ X	3J	9.4	0.7
$\begin{array}{c} \text{H} & \text{H} \\ & \backslash / \\ & \text{C}=\text{C} \\ & / \backslash \\ \text{H} & \text{X} \end{array}$	$^3J_{\text{cis}}$	24.5	4.2
	$^3J_{\text{trans}}$	27.3	3.5
$\begin{array}{c} \text{H} & \text{H} \\ & \backslash / \\ & \text{C} \\ & / \backslash \\ \text{H} & \text{X} \\ \text{Cl} & \text{Cl} \end{array}$	$^3J_{\text{cis}}$	17.7	2.4
	$^3J_{\text{trans}}$	13.6	2.8
	$^3J_{\text{cis}}$ or J_{BC}	12.6	1.4
	$^3J_{\text{trans}}$ or J_{AC}	8.8	1.7

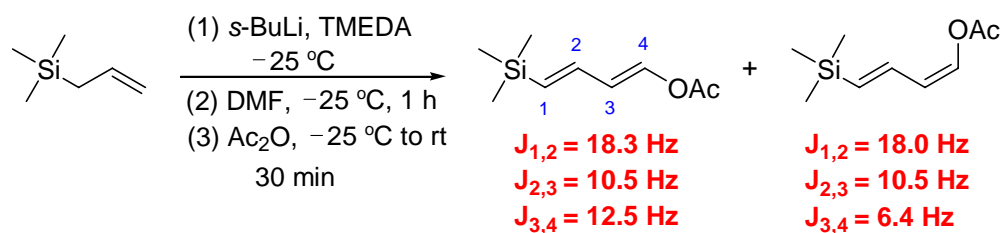
(4) 3J (sp^2-sp^2)



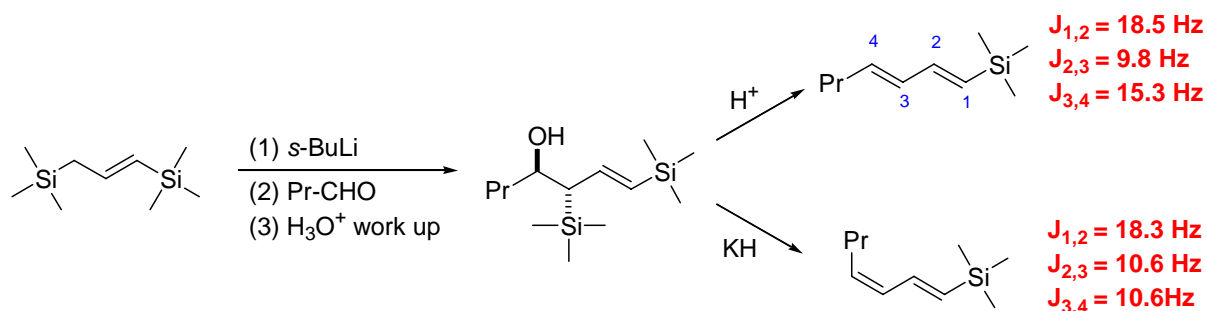
12~18 Hz $^3J_{trans} > ^3J_{cis}$ 6~12 Hz

Examples

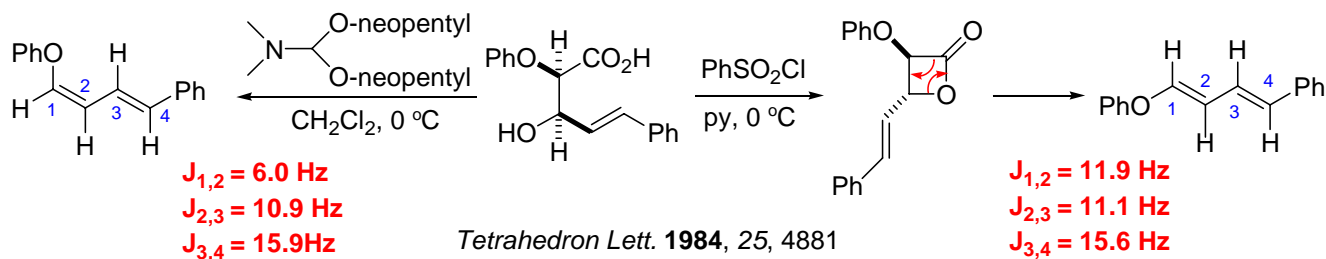
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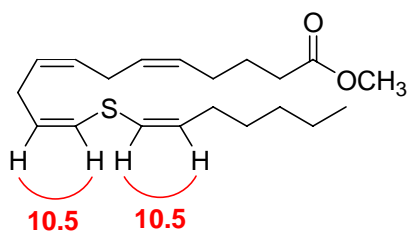
②



③



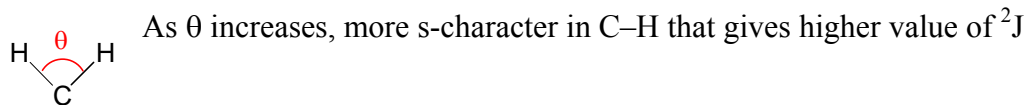
④



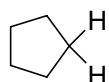
3-2. Geminal H-H Couplings (${}^2J_{\text{HH}}$): $-20 \sim +40$ Hz

(1) Factors that influence the value of 2J

a. S-P Hybridization



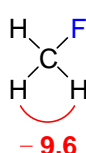
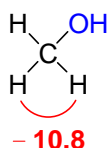
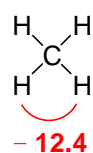
Methane (CH_4) sp^3 ${}^2J = -12.4$ Hz Ethylene ($\text{CH}_2=\text{CH}_2$) sp^2 ${}^2J = +2.5$ Hz



b. Electronegative atom in α -position leads to a positive shift in ${}^2J_{\text{HH}}$ (Inductive effect)

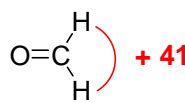
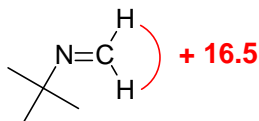
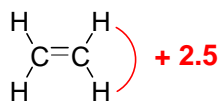
Examples

①



Electronegative atoms withdraw electrons of p-character leaving more s-character in C-H bond.

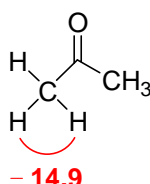
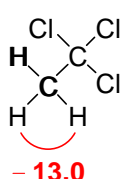
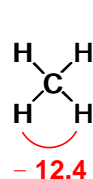
②



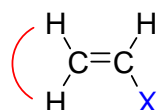
c. Electronegative atom in β -position leads to a negative shift in ${}^2J_{\text{HH}}$

Example

①

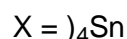


② sp^2 H's



$${}^2J = 8.5 - 3E_x$$

E_x : Electronegativity



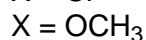
$+ 2.8$ Hz



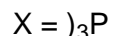
$- 1.4$ Hz



$+ 2.5$ Hz



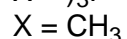
$- 2.0$ Hz



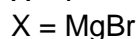
$+ 2.02$ Hz



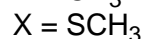
$- 3.2$ Hz



$+ 2.08$ Hz



$+ 7.4$ Hz




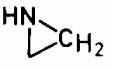
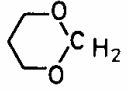
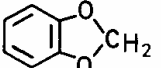
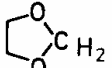
$- 0.3$ Hz



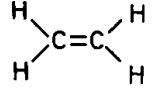
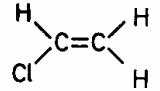
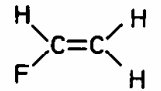
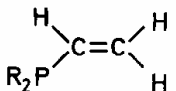
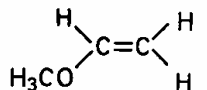
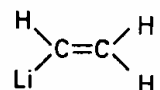
$+ 7.1$ Hz

Table 4.10 The influence of substituents on geminal-coupling constants

1. α -Substitution

CH_4	- 12.4		+ 5.5
CH_3Cl	- 10.8	$\text{RN}=\text{CH}_2$	+ 16.5
CH_2Cl_2	- 7.5	$\text{O}=\text{CH}_2$	+ 42.2
	+ 2.0		- 6
	± 1.5		0

2. β -Substitution

	+ 2.5		- 1.4
	- 3.2		+ 2.0
	- 2.0		+ 7.1

3. Adjacent π bonds

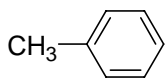
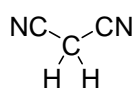
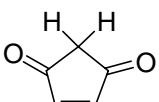
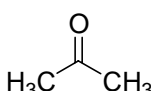
CH_3CN	- 16.9		- 14.5
$\text{CN}-\text{CH}_2-\text{CN}$	- 20.4		

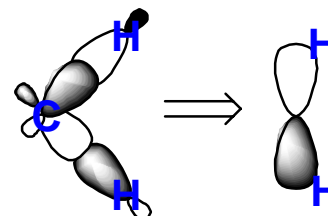
d. Hyper-conjugation effects

Electron withdrawing substituents which take electrons from antisymmetric orbitals of CH_2 give **negative contribution**.

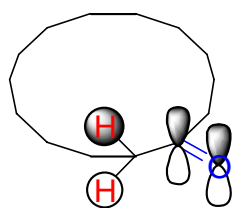
Examples

①

CH_4	${}^2J = -12.4 \text{ Hz}$	CH_3-CN	- 19.2 Hz
	- 14.5 Hz		- 20.3 Hz
	- 21.5 Hz		- 14.9 Hz



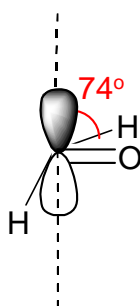
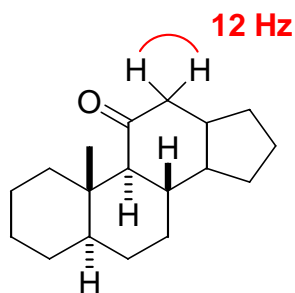
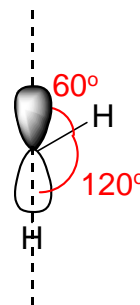
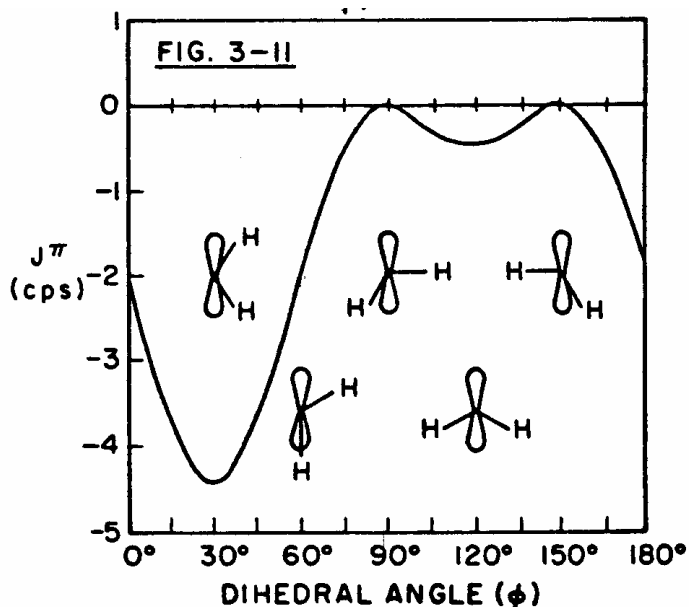
②



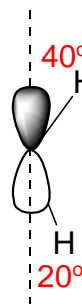
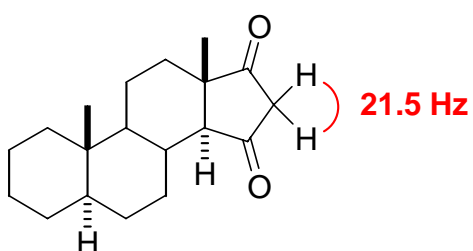
$${}^2J_{HH} = {}^2J_{HH}(\sigma) + {}^2J_{HH}(\pi)$$

-12.4 Hz Hyperconjugation

Barfield, M. *J. Am. Chem. Soc.* **1963**, 85, 1899.



${}^2J(\pi) = \sim 0-1$ Hz



${}^2J(\pi) = 4$ Hz

total ${}^2J(\pi) = 2 \times 4$ Hz = 8 Hz
two carbonyl groups

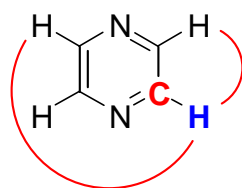
◆ **Determination of J_{HH} when two protons are chemically equivalent**

① Use JHD

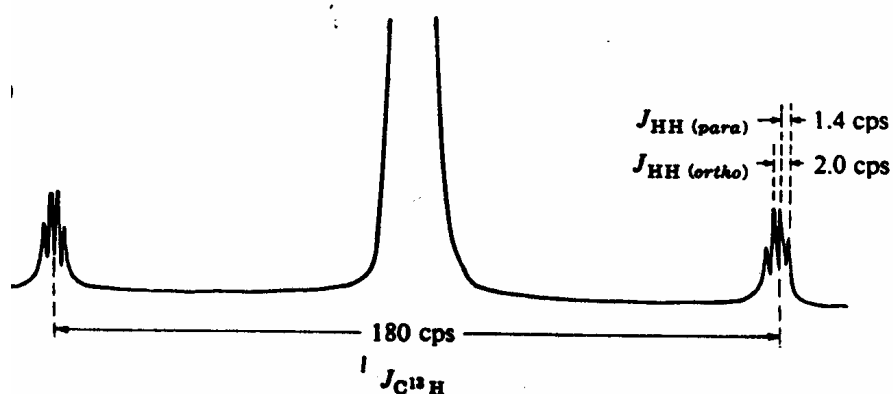
$J_{HH} = 6.514 \times J_{HD}$

$\text{CHDCl}_2 \quad J_{HD} = -1.15 \text{ Hz} \quad \therefore J_{HH} = (-1.15) \times 6.514 = -7.5 \text{ Hz}$

② Use ^{13}C -satellites



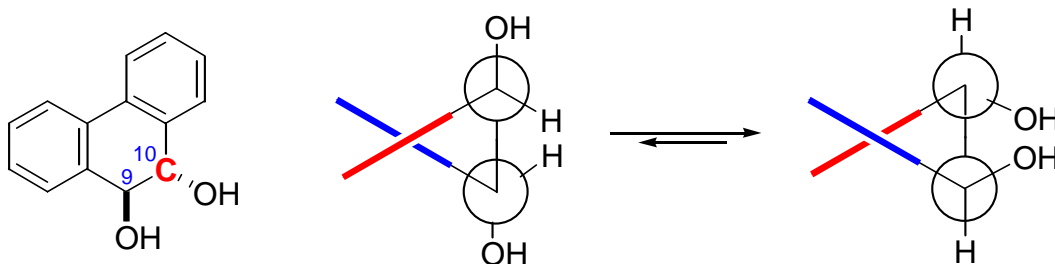
Pyrazine



Carbon 13 satellite spectrum of pyrazine.

^3J from ^{13}C -satellite proton resonance

J. Org. Chem. **1983**, *48*, 4139



	$\text{H}_9, \text{H}_{10} \delta$ (ppm)	$^3\text{J}_{9,10}$ (Hz)	$^1\text{J}_{\text{H-C}}$ (Hz)
Diol	4.61	10.4	142.2
Diacetate	6.07	5.6	152.5

3-3 Long-range couplings

Review:

Chem. Rev. **1969**, *69*, 757.

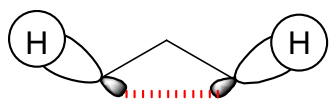
Pure & Appl. Chem. **1964**, *14*, 15.

(1) Sigma (σ) – bond couplings

$$^2\text{J} \geq ^3\text{J} \gg ^4\text{J}$$

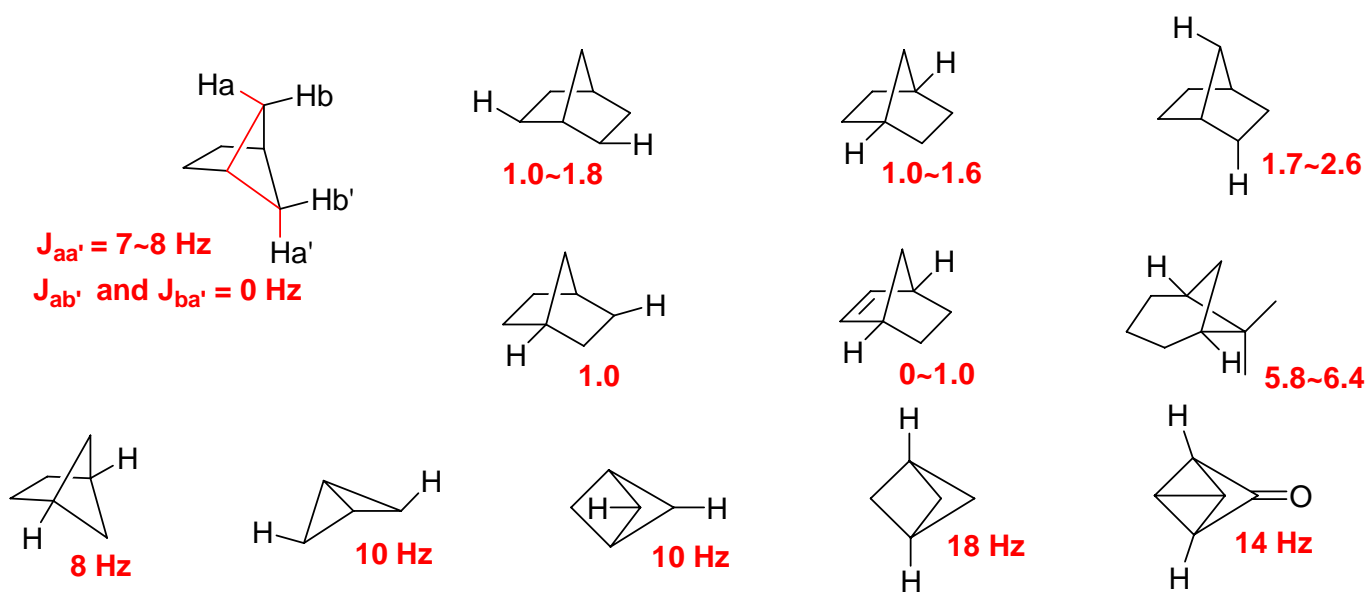
4~12 Hz usually 0 Hz

a. W-letter Rule or W-coupling (or M-coupling)



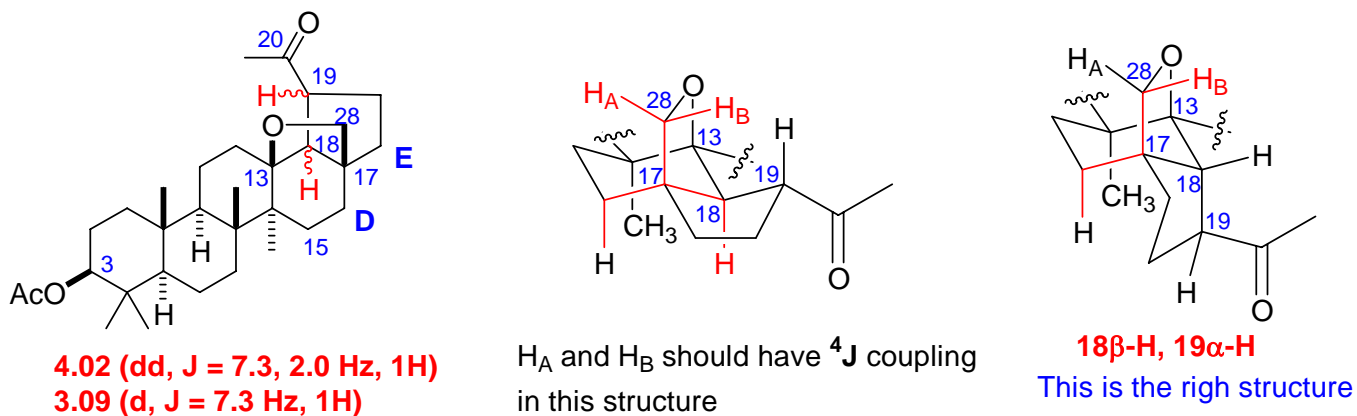
J. Am. Chem. Soc. **1961**, *83*, 2769.

Examples

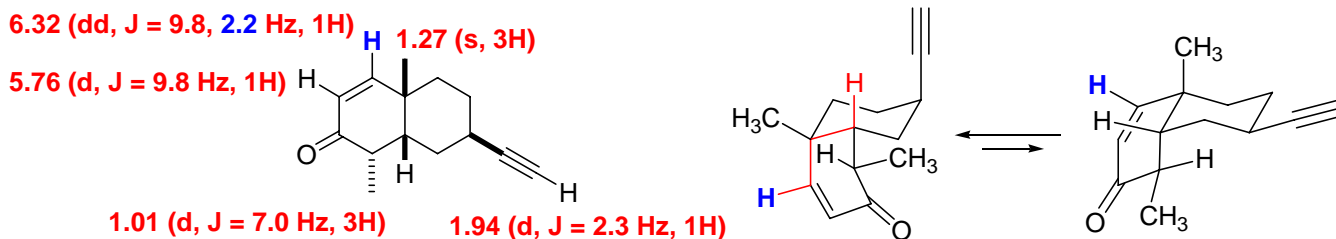


Stereochemical applications

① 3 β -acetoxy-20-oxo-13 β ,28-epoxy-30-lupane (Ring D/E junction: cis or trans?)

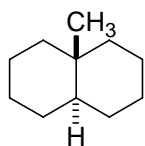


② Structure of chamaecynone (*Tetrahedron Lett.* 1966, 3663)

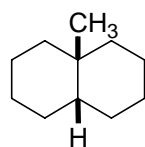


b. $\Delta W_{1/2} = W_{1/2}(\text{Me}) - W_{1/2}(\text{TMS})$

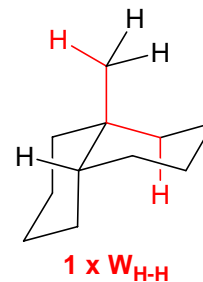
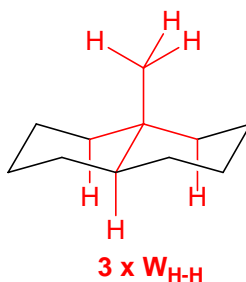
①



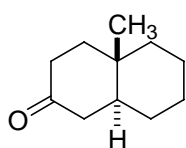
trans - $\Delta W_{1/2} = 0.65 \text{ Hz}$



cis - $\Delta W_{1/2} = 0.15 \sim 0.30 \text{ Hz}$

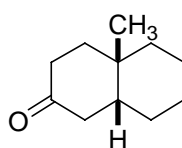


②

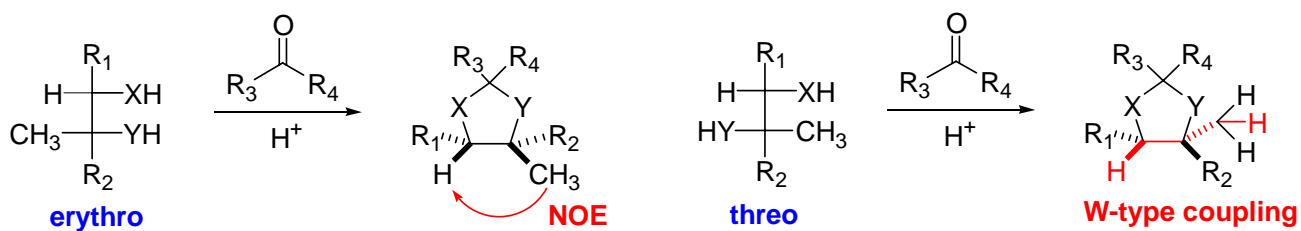


trans - $\Delta W_{1/2} = 1.05 \text{ Hz}$

cis - $\Delta W_{1/2} = 0.35 \text{ Hz}$

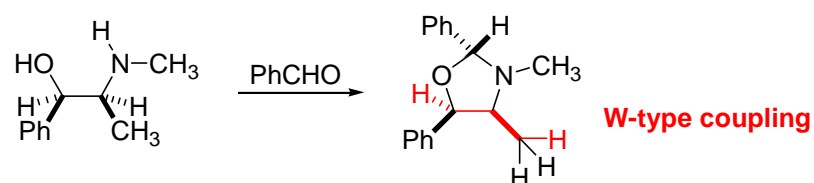


c. To distinguish **threo** and **erythro** isomers of certain α -glycols and related compounds

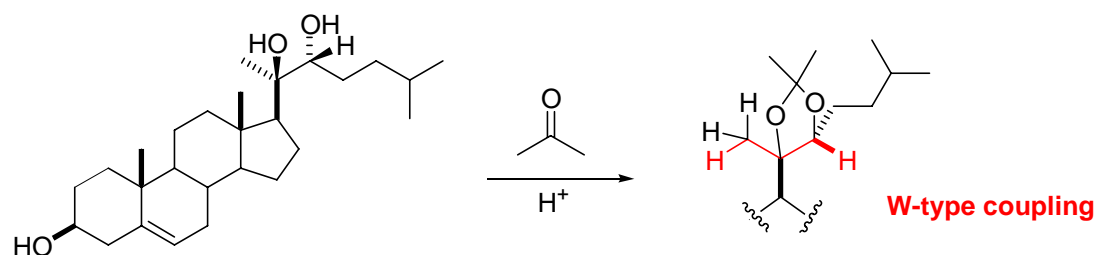


Examples

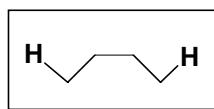
① (-)-ephedrine



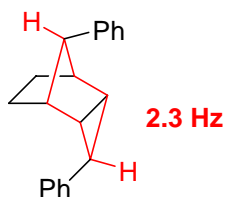
②



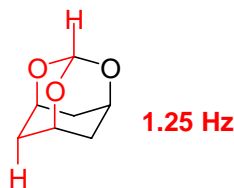
(2) 5J σ -bond couplings



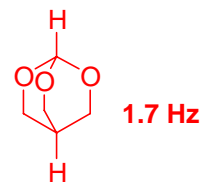
0.5 ~ 1.0 Hz



2.3 Hz



1.25 Hz



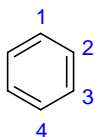
1.7 Hz

(3) Coupling in unsaturated systems

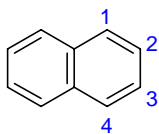
a. Aromatic compounds

$$J_{AB} = J_{AB}(\pi) + J_{AB}(\sigma)$$

$J_{AB}(\pi)$: generally small (~ 2 Hz); not much change in bond order of π orbital (P_{AB}).



$P_{A,B}$		$J_{AB}(\pi)$ calculated	J_{AB} (total) observed
$P_{1,2}$	0.67	0.80	8~9
$P_{1,3}$	0.00	0	2~5
$P_{1,4}$	-0.17	0.05	0.5



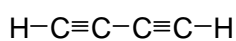
$P_{A,B}$		$J_{AB}(\pi)$ calculated	J_{AB} (total) observed
$P_{1,2}$	0.72	0.95	8.6
$P_{2,3}$	0.60	0.66	6.0
$P_{1,3}$	0.00	0	1.4
$P_{1,4}$	-0.36	0.23	0.6

b. Unsaturated **non-aromatic** compounds

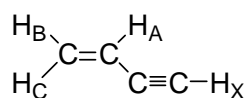
Karplus, M. *J. Am. Chem. Soc.* **1960**, 82, 4432.

	$J_{AB}(\pi)$	$J_{AB} (J_{AB}^{\pi} + J_{AB}^{\sigma})$
H-C=C-H	+1.5	+7 ~ +18
H-C≡C-H	+4.6	+9.1
H-C=C-C-H	-1.7	-1.4 ~ -1.8
H-C≡C-C-H	-3.7	-2.3
H-C=C=C-H	-6.7	-7.0 ~ -6.1
H-C-C=C-C-H	+2.0	+2.0
H-C-C≡C-C-H	+2.9	+2.7
H-C=C=C=C-H	+7.8	+8.95

Examples



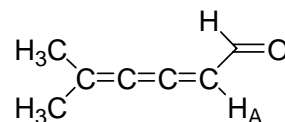
$$|J| = 2.2 \text{ Hz}$$



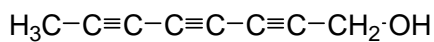
$$J(\text{H}_A, \text{H}_X) = -2.1 \text{ Hz}$$

$$J(\text{H}_B, \text{H}_X) = 0.8 \sim 0.9 \text{ Hz}$$

$$J(\text{H}_C, \text{H}_X) = 0.7 \text{ Hz}$$

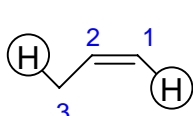


$$|J(\text{CH}_3, \text{H}_A)| = 1.2 \text{ Hz}$$

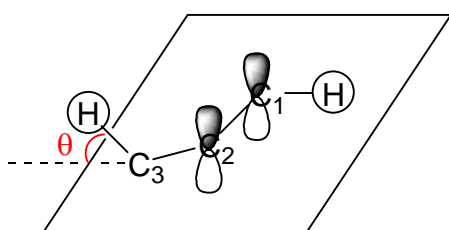


$$|J| = 0.4 \text{ Hz } (^9J)$$

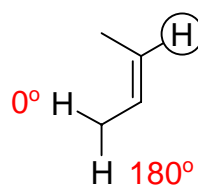
c. Allylic coupling



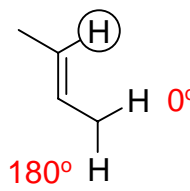
Angle dependency



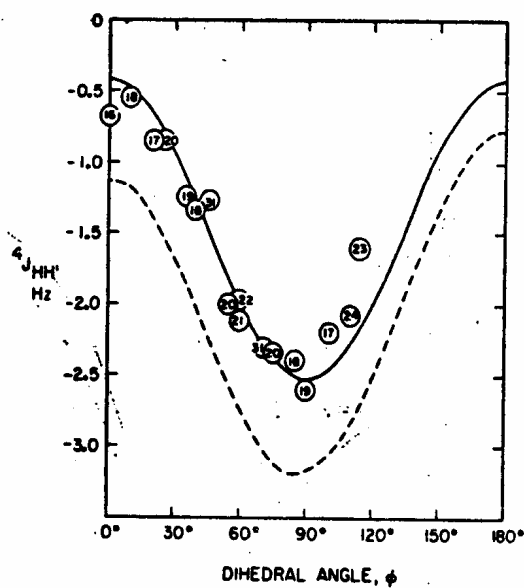
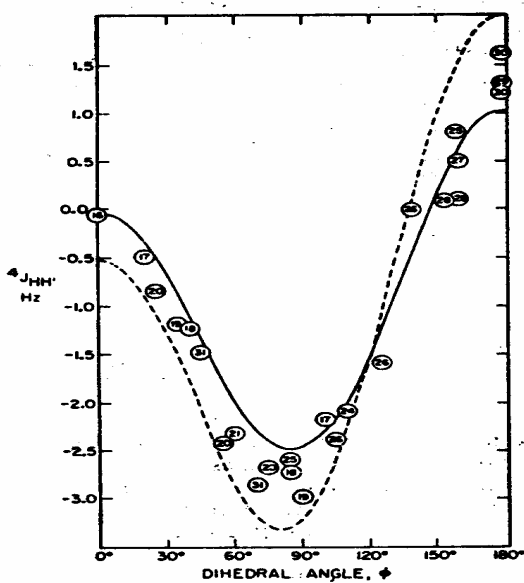
$|J|$: maximum when $\theta = 90^\circ$



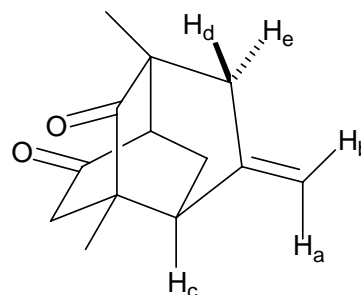
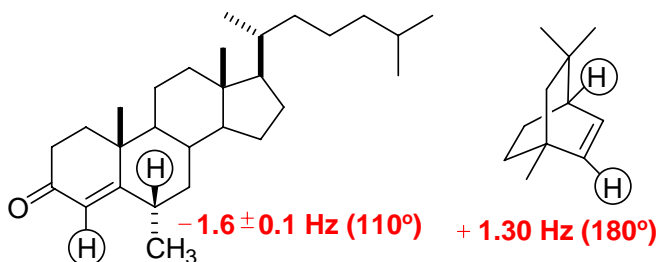
transoid (left)



cisoid (right)



Examples



$$J_{a,c} = -0.55 \text{ Hz } (10^\circ) \text{ c}$$

$$J_{b,c} = -0.2 \text{ Hz } (10^\circ) \text{ t}$$

$$J_{a,d} = -1.18 \text{ Hz } (35^\circ) \text{ t}$$

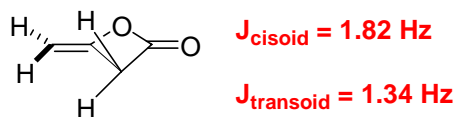
$$J_{b,d} = -1.24 \text{ Hz } (35^\circ) \text{ c}$$

$$J_{a,e} = -2.97 \text{ Hz } (90^\circ) \text{ t}$$

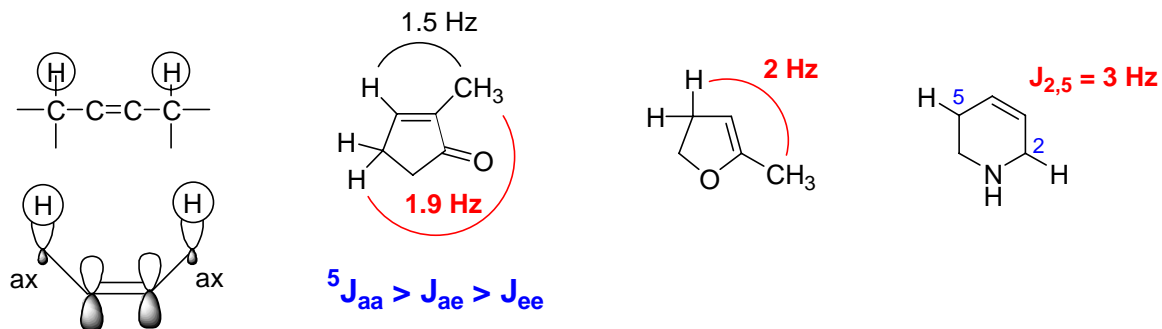
$$J_{b,e} = -2.60 \text{ Hz } (90^\circ) \text{ c}$$

Generally, transoid coupling > cisoid coupling

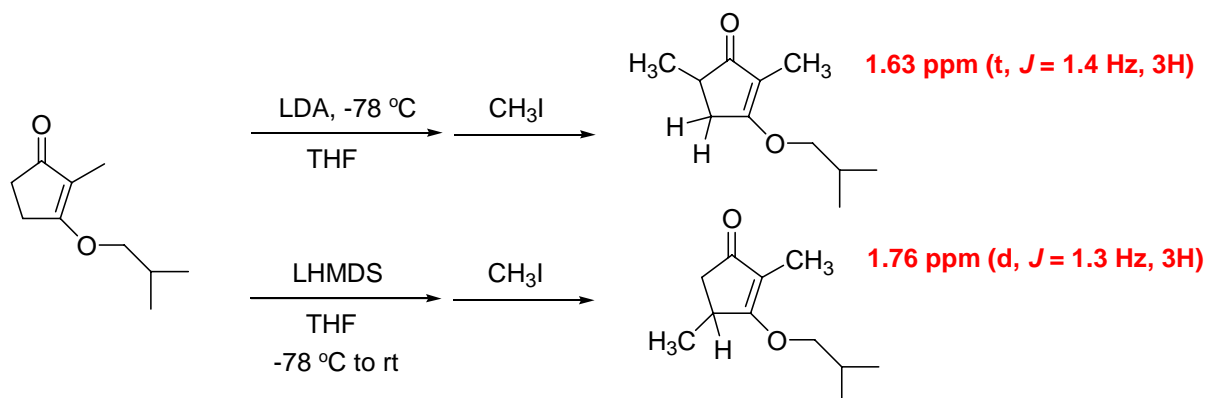
<exceptions>



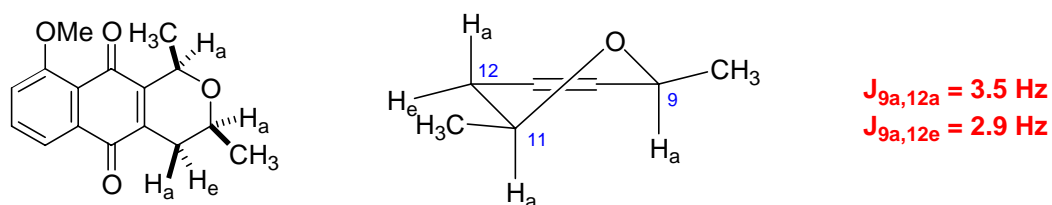
d. Homoallylic coupling: ${}^5J = 0.6 \sim 3.0 \text{ Hz}$



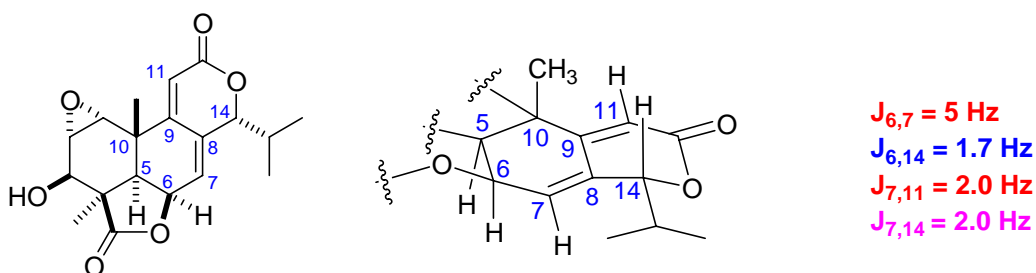
①



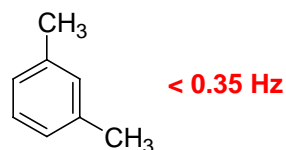
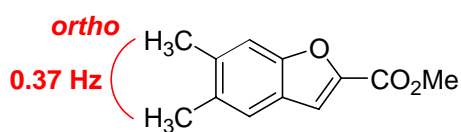
②



③

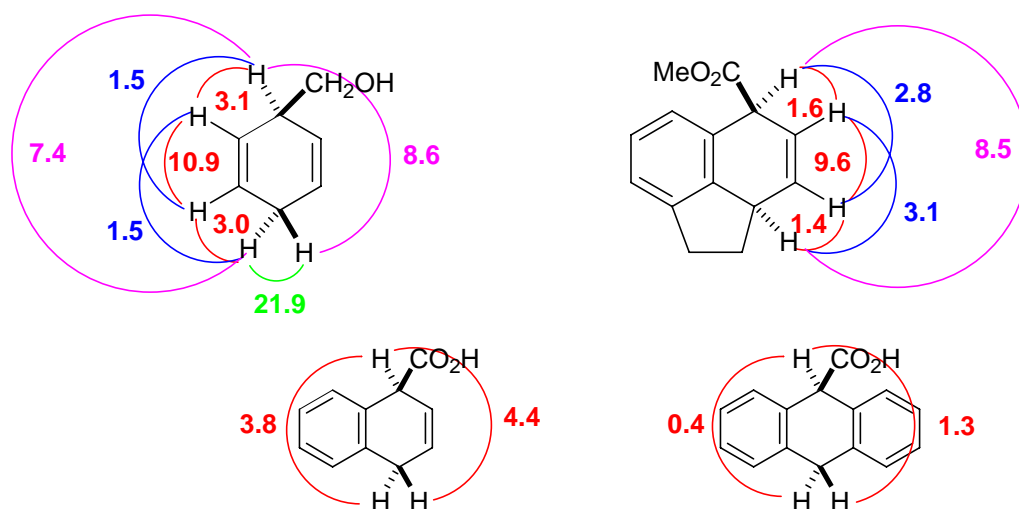
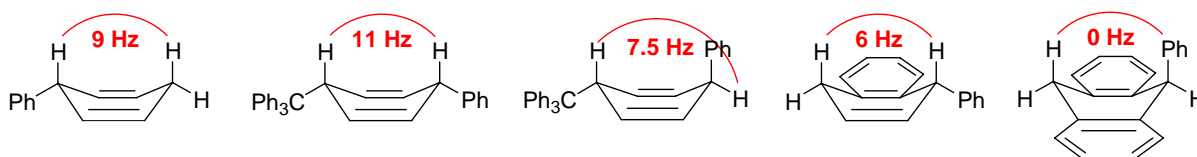


④ Interbenzylic couplings

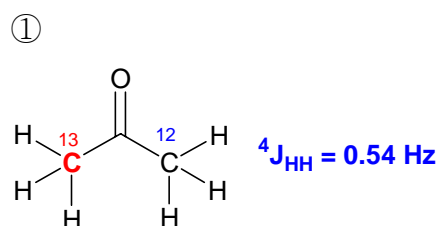
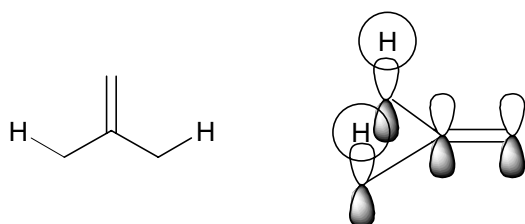


1/3 of typical homoallylic couplings

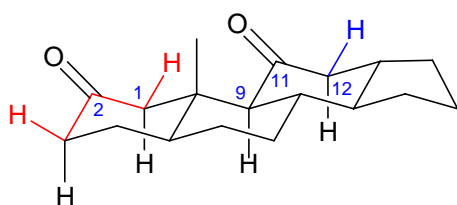
⑤ 1,4-Dihydrobenzene systems – |J|: usually large



e. "Pseudoallylic" coupling



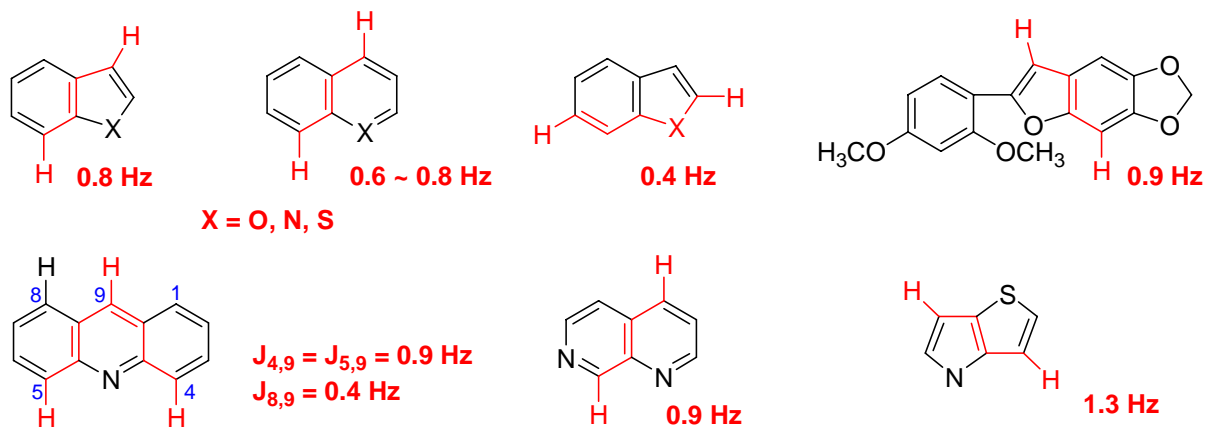
②



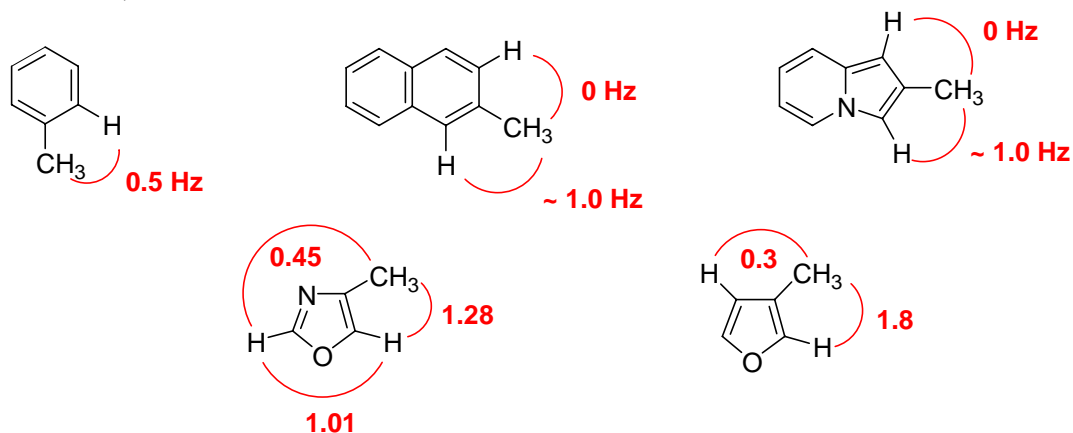
3.52 ppm (dd, $J = 13.5, 2.0 \text{ Hz}$, 1H)
2.26 ppm (d, $J = 12 \text{ Hz}$, 1H, 12 β -H)
1.90 ppm (d, $J = 12 \text{ Hz}$, 1H, 12 α -H)

f. Long-range couplings in polycyclic aromatic systems

① polynuclear heterocyclic system: zig-zag path

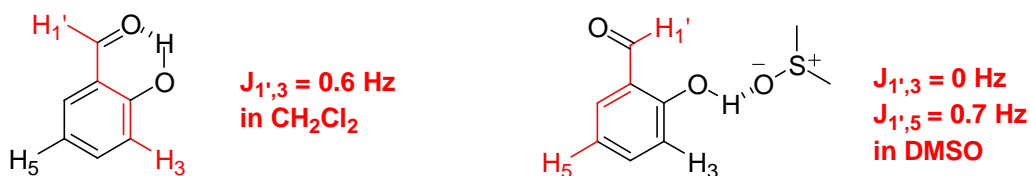


② $J_{\text{Ar-CH,Ar-H}}$: Stronger J if coupled via a “localized” double bond.

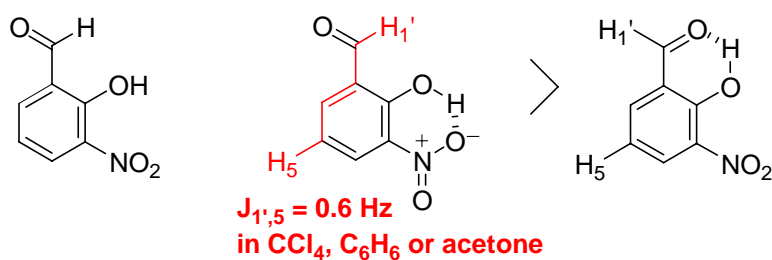


g. Zigzag couplings in simple aromatic phenols

①



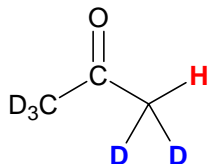
②



3-4. $^2J_{HD}$: small and broad

D: 0.015% Natural abundance; H: 99.985 %

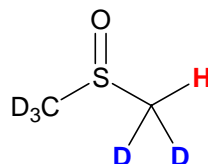
D: I (spin quantum number) = 1, possible spin states = -1, 0, +1 \rightarrow triplet



$^2J_{HD} = 2.3$ Hz, quintet (5)

Possible spin state = -2, -1, 0, +1, +2

Only $^2J_{HD}$ can be detected.



$^2J_{HD} = 1.9$ Hz, quintet

※ Isotope Chemical Shift

- ① CH_4
 CH_3D 0.019 ± 0.001 ppm up-field shift
 CH_2D_2 0.027 ± 0.003
 CHD_3 0.045 ± 0.004
- ② CH_3COCH_3
 CD_3COCH_2D 0.034 ± 0.001 ppm up-field shift
- ③ $^{12}CF_3H$
 $^{13}CF_3H$ 0.126 ppm up-field shift

3-5. $^{14}N-H$ Coupling

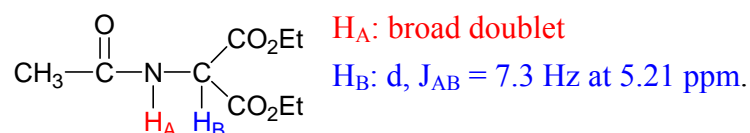
^{14}N : Natural abundance 99.63%; I (spin quantum number) = 1

$^1J_{14N-H}$

- a. Fast exchanging H: sharp and singlet without N-H coupling
- b. Slow exchanging H: broad peak around 2.0~2.4 ppm (quadrupole relaxation)
cf. amide-H: 6-9 ppm
- c. R_3N^+-H : $^1J_{+N-H} = \sim 50-60$ Hz, triplet (broad)

Examples

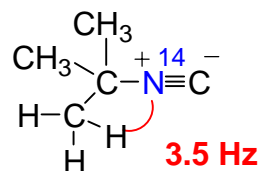
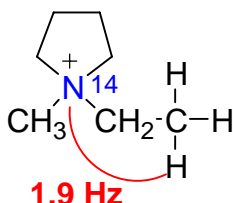
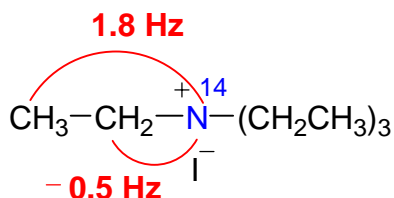
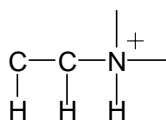
①



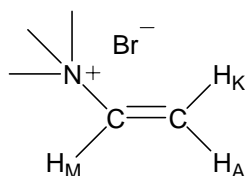
② $CH_3CH_2CH_2NH_3^+$

$^1J_{14NH} = \sim 50$ Hz at 6.7 ppm

${}^2J_{14N-H}$ and ${}^3J_{14N-H}$: Only with $R_4{}^{14}N^+$
 ${}^1J_{14N-H} > 0$; ${}^2J_{14N-H} < 0$; ${}^3J_{14N-H} > 0$;



▪ NMR spectrum of



$${}^3J_{14NHA} = 5.5 \text{ Hz} \quad {}^3J_{14NHK} = 2.6 \text{ Hz} \quad |{}^2J_{14NHM}| = 3.5 \text{ Hz}$$

$$|{}^2J_{14NCH3}| = 0.5 \text{ Hz} \quad {}^3J_{HKHM} = 14.8 \text{ Hz} \quad {}^3J_{HAHM} = 8.3 \text{ Hz} \quad {}^2J_{HAHK} = -4.1 \text{ Hz}$$

3-6. ${}^{15}N-H$ Coupling

${}^{15}N$: Natural abundance = 0.36%; I (spin quantum number) = 1/2

${}^{15}N$ -enriched compounds should be prepared!

$$\%S = 0.43 \times {}^1J({}^{15}N-H) - 6$$

$$\%S = 100 \cos\phi(\cos\phi - 1) \quad \phi: \text{bond angles between N and its substituents}$$

${}^+NH_4$: $\phi = 107.3^\circ \rightarrow 22.9\%$ S-character

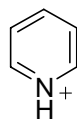
${}^+NH_4$: ${}^1J_{15NH} = 73.2 \text{ Hz} \rightarrow 25.47\%$ S-character

${}^1J_{15NH}$

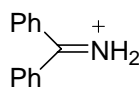
$-NH_2$ **62 Hz (20.7)**

$R-NH_3^+$ **73-76 Hz (26.7)**

$R-C(=O)-NH_2$ **88-92 Hz (33.6)**



90 Hz (32.7)



92.6 Hz (33.3)

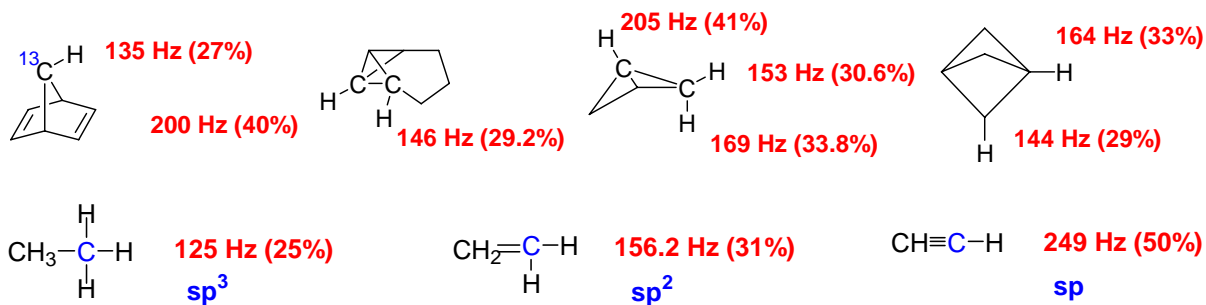
3-7. ${}^{13}C-H$ Coupling

${}^{13}C$: Natural abundance 1.11%;

I (spin quantum number) = 1/2

S-character of C-H bond

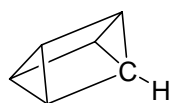
$$\%S = 0.20 \cdot {}^1J_{13C-H}$$



Based on INDO-MO calculation,

Improved equation

$$\%S = (^1J_{13CH} + 18.4)/5.7$$



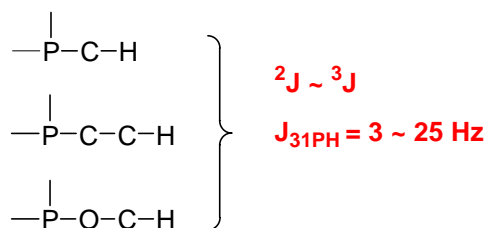
Calculated $^1J_{13CH} = 189$ Hz

Observed $^1J_{13CH} = 180$ Hz

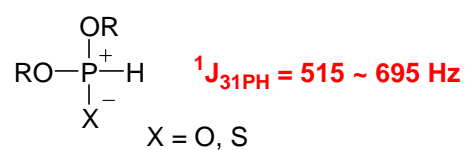
3-8. $^{31}\text{P-H}$ Coupling

^{31}P : Natural abundance 100%; I (spin quantum number) = 1/2

$^2J \sim ^3J$

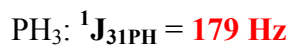


1J

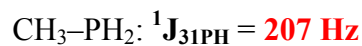


Examples

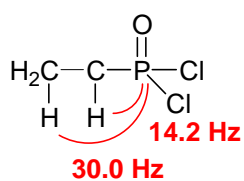
①



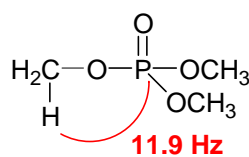
②



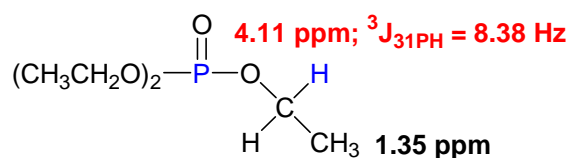
③



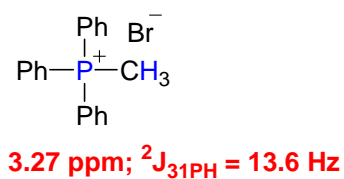
④



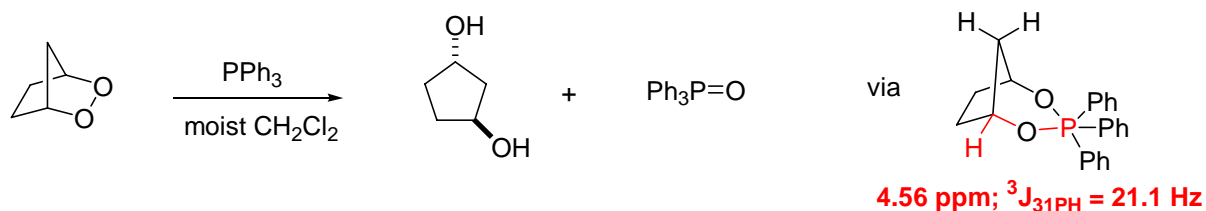
⑤



⑥



J. Org. Chem. **1981**, *46*, 4105.



3-9. ^{19}F -H Coupling

^{19}F : Natural abundance 100%;

I (spin quantum number) = 1/2

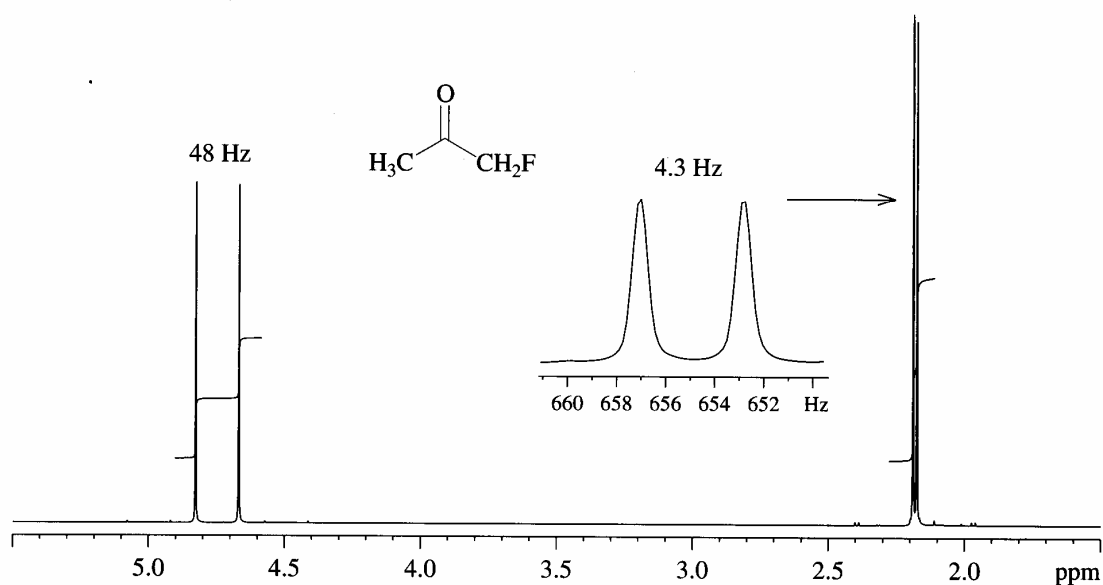
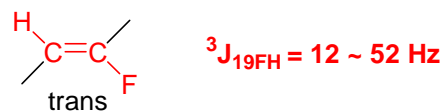
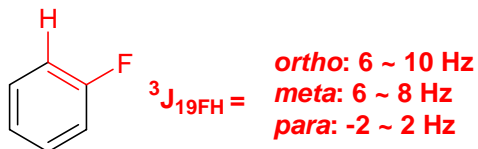
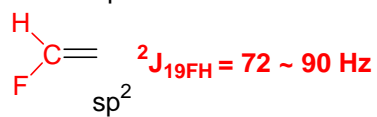
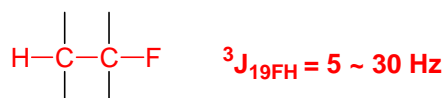
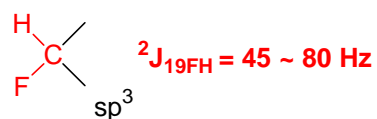
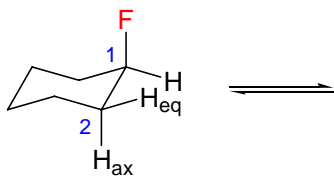


FIGURE 3.42 ^1H spectrum of fluoroacetone in CDCl_3 at 300 MHz.

Examples

①

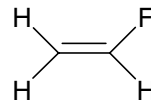


$${}^2J_{H1F} = 49 \text{ Hz}$$

$${}^3J_{H2axF} = 43.5 \text{ Hz}$$

$${}^3J_{H2eqF} < 3 \text{ Hz}$$

②



$${}^3J_{HFcis} = 20.1 \text{ Hz}$$

$${}^3J_{HFtrans} = 52.4 \text{ Hz}$$

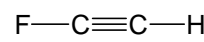
$${}^3J_{HFgem} = 84.7 \text{ Hz}$$

$${}^2J_{H1F} = 49 \text{ Hz}$$

$${}^3J_{H2axF} < 3 \text{ Hz}$$

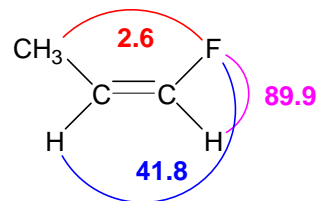
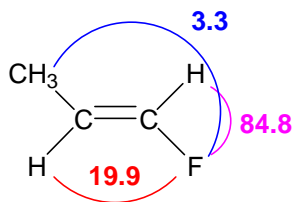
$${}^3J_{H2eqF} < 3 \text{ Hz}$$

③

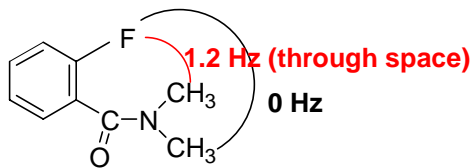


$${}^3J_{FH} = 21 \text{ Hz}$$

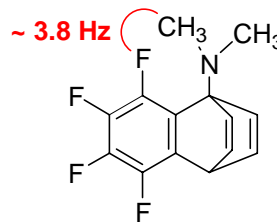
④



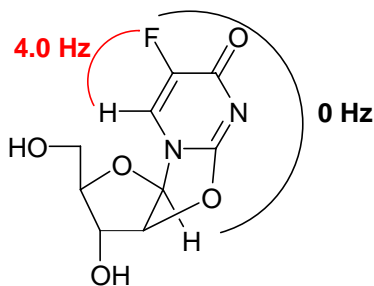
⑤



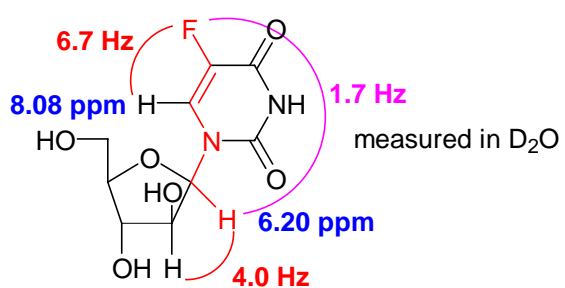
⑥



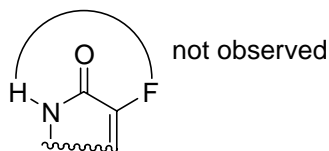
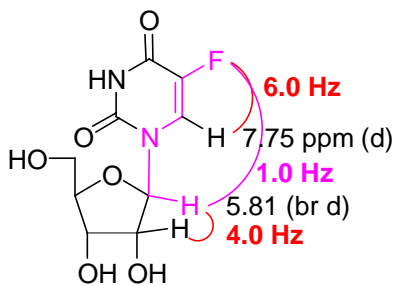
⑦



⑧



⑨



4. Environmental Effect

4.1 Sample

$$\text{Sensitivity} \propto N \cdot \{(I + 1)/I^3\} \mu^3 \cdot B_0^2$$

Relative sensitivity:	^1H	1.00
	^{19}F	0.834
	^{13}C	0.0159
	^2H	0.0096

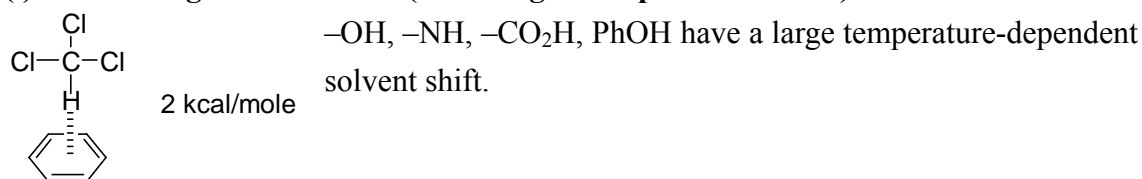
4.2 Solvent Effect

- Solvent effect on the **external standard** – Sample peaks move on the solvent used, but no effect on the external standard (reference).
- Solvent effect on the **internal standard** – Both sample and the reference peaks are subjected to the solvent effect.

► Chemical interaction with a solvent

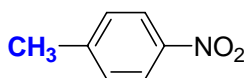
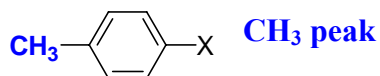
(a) Solvation

(i) H-bonding with a solvent (including π -complex formation)



► Solvation with benzene

①

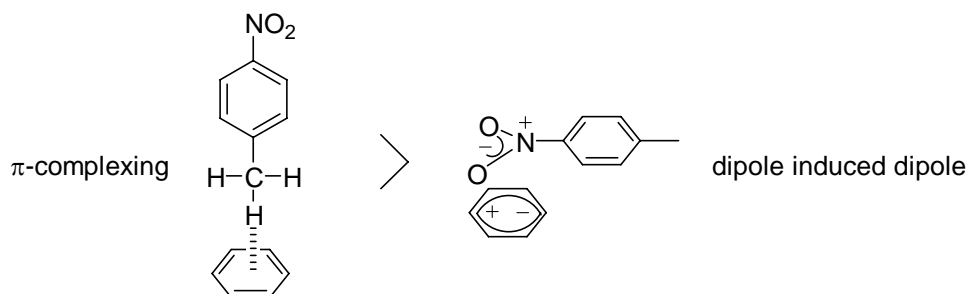


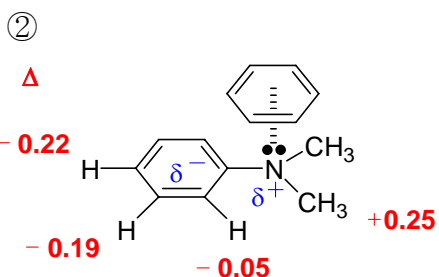
$$\Delta = \delta(\text{in CCl}_4) - \delta(\text{in benzene})$$

Δ is largest when $X = \text{NO}_2$

Most **deshielded** in CCl_4 ; most **shielded** in benzene

← →



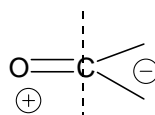
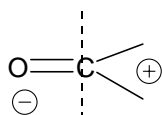
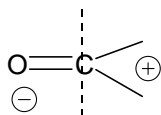


③ Carbonyl reference plane rules

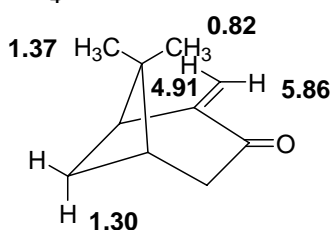
a. C_6D_6/CCl_4

b. C_5D_5N/CCl_4

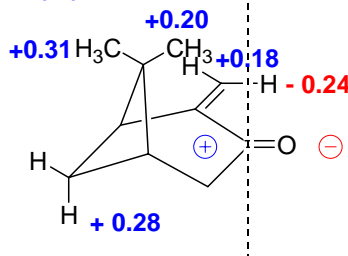
c. C_6F_6/CCl_4



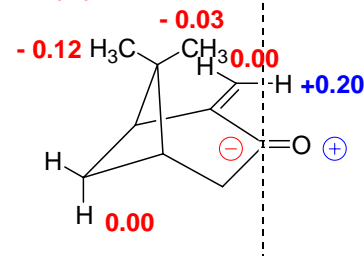
In CCl_4



In C_6D_6

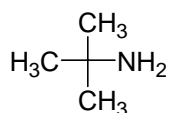
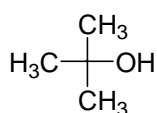


In C_6F_6



(ii) Indirect solvent effect caused by solvation on the near-by functional groups

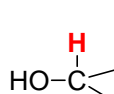
①



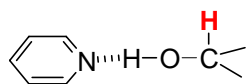
Solvation to $-OH$ and $-NH_2 \rightarrow$ chemical shift of $t-Bu$ will be perturbed.

CH_3 's are non-equivalent

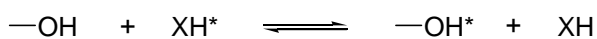
②



Chemical shift in CCl_4 and in pyridine are different.



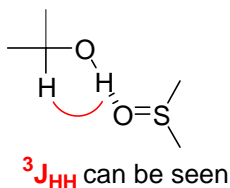
(b) Proton exchange ($-OH$, $-NH_2$, -----)



$$\tau^* = \sqrt{2}/(\pi \cdot \Delta\nu)$$

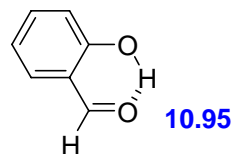
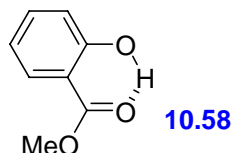
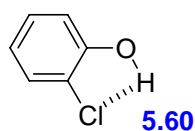
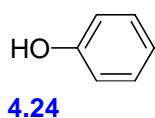
τ^* : life time; $\Delta\nu$: chemical shift difference between $-OH$ and $-XH^*$ in Hz

Solvent effect: fixation of exchangeable H's by forming strong H-bond with DMSO or acetone.



※ Add D₂O to make sure of the presence of alcoholic proton.

Intramolecular H-bonding (δ in cyclohexane)



5. Chemical Shift – semi-quantitative considerations

5.1. Factors responsible for chemical shifts

$$H_{\text{effect}} = H_0 \cdot (1 - \sigma)$$

σ = shielding constant: $4\pi e^2 / (3mc^2) \int r\rho(r) dr = 17.8$ ppm for H

If a hydrogen atom is placed in an electric field E (in esu unit),

$$\Delta\sigma = - (881/226) \cdot (a^3 E^2 / mc^2) = - 0.74 \times 10^{-18} E^2 \text{ (downfield shift)}$$

a: Bohr radius, 0.529×10^{-8} cm for H

m: weight of electron

Examples

(a) a unit charge located at 1 Å, 1.5 Å, 2 Å

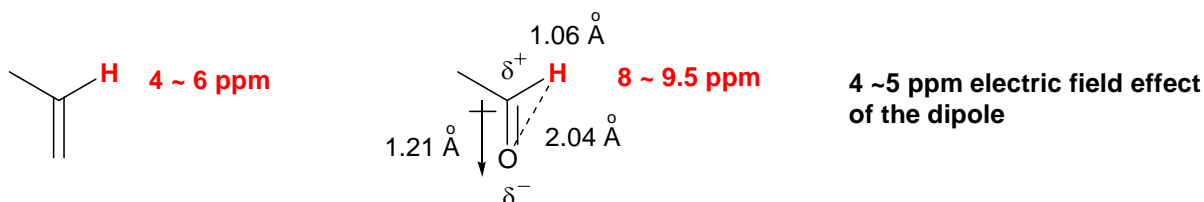
$$E = 4.8 \times 10^6, 2.14 \times 10^6, 1.2 \times 10^6 \text{ esu}$$

$$\Delta\sigma = 17 \text{ ppm}, 3.4 \text{ ppm}, 1.1 \text{ ppm downfield shift}$$

(b) a dipole

$$E = \mu(1 + 3\cos^2\theta)^{1/2} / R^3$$

μ : dipole moment, R: distance



Dipole moment of C=O is ca. 2×10^{-10} esu

$$\sigma_E = - 4.6 \times 10^{-6} \text{ (4.6 ppm downfield shift by the C=O dipole)}$$

① Local diamagnetic effects

Dailey, Shoolery rule

CH₃-CH₂-X system

$$\begin{aligned} \text{Electronegativity of X} &= 0.684 \cdot (\delta_{\text{CH}_2} - \delta_{\text{CH}_3}) + 1.78 && \text{in ppm} \\ &= 0.02315 \cdot (\Delta\text{CH}_3 - \Delta\text{CH}_2) + 1.71 && \text{in Hz} \end{aligned}$$

Assumption

- 1) paramagnetic contribution ≈ 0
- 2) neighboring atom's contribution \approx constant

② Paramagnetic effects – **induced dipole by polarizable atom** (directional)

“Due to non-spherical electron distribution of the particular atom” \rightarrow downfield shift

※ Temperature-independent paramagnetism

※ Paramagnetic effects can be neglected in ¹H NMR, but important for ¹³C, ¹⁹F NMR.

③ **The magnetic anisotropy effect** of neighboring groups

Magnetic susceptibility (χ)

$$\mu = \chi H_0$$

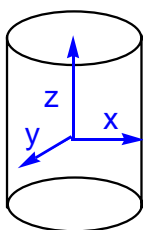
μ : Induced magnetic dipole moment in H_0 .

χ directional

► If $\chi_{xx} = \chi_{yy} \neq \chi_{zz}$

$$\Delta\chi_z = \chi_{zz} - \chi_{yy} = \chi_{zz} - \chi_{xx}$$

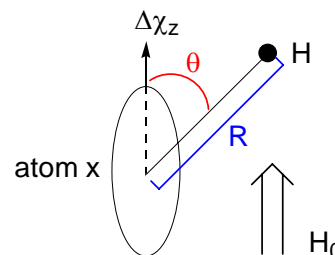
$\Delta\chi_z$: Anisotropy of χ



In a magnetic field H_0 ,

H atom experiences secondary magnetic field H'

$$H' = -H_0 \cdot \Delta\chi_z (1 - 3\cos^2\theta) / 3R^3 \quad \text{McConnell's equation}$$



“Anisotropy shift”

$$\Delta\sigma = -H'/H_0 = \Delta\chi_z (1 - 3\cos^2\theta) / 3R^3$$

If $\Delta\chi_z < 0$; $3R^3 > 0$;

The sign of $\Delta\sigma$ depends on the value of $(1 - 3\cos^2\theta)$

When $\theta = 55^\circ 44'$ $\Delta\sigma = 0$

$\Delta\sigma > 0 \rightarrow$ + up-field shift (shielding)

$\Delta\sigma < 0 \rightarrow$ - down-field shift (deshielding)

► If $\chi_{xx} \neq \chi_{yy} \neq \chi_{zz}$

$$\Delta\chi_z = \chi_{zz} - \chi_{yy}$$

$$\Delta\chi_x = \chi_{xx} - \chi_{yy}$$

$$\Delta\sigma = \Delta\sigma_z + \Delta\sigma_x$$

$\Delta\chi < 0$ when $\chi_{zz} > \chi_{xx}$ or χ_{yy}

(a) $C \equiv X$ The shielding zone (cone)

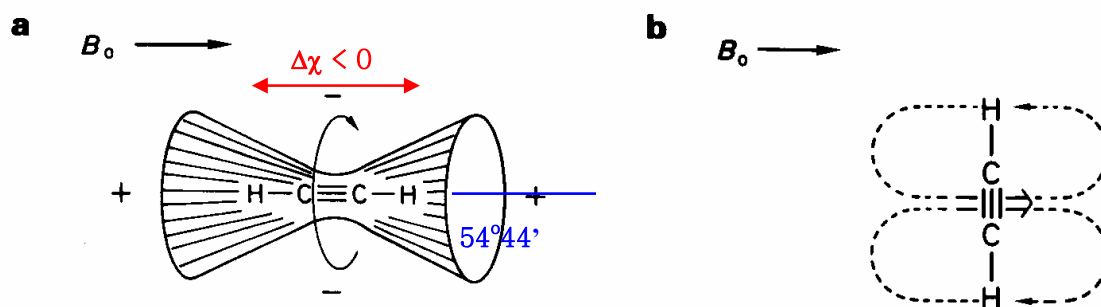
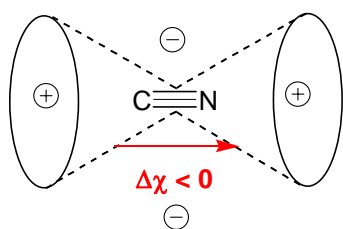
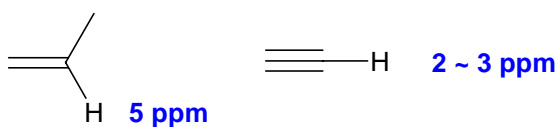


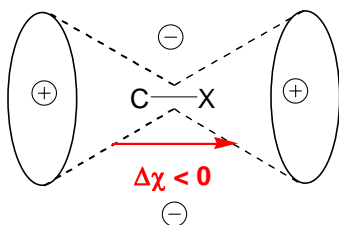
Figure 4.8 Schematic representation of the magnetic anisotropic effect of the triple bond



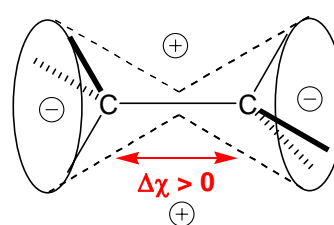
e.g.



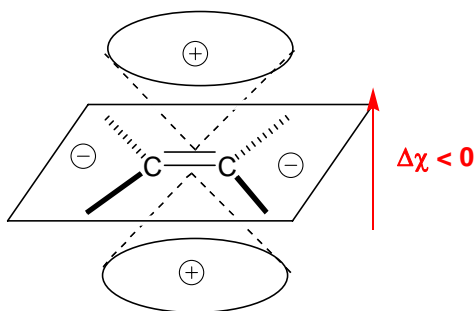
(b) C-X



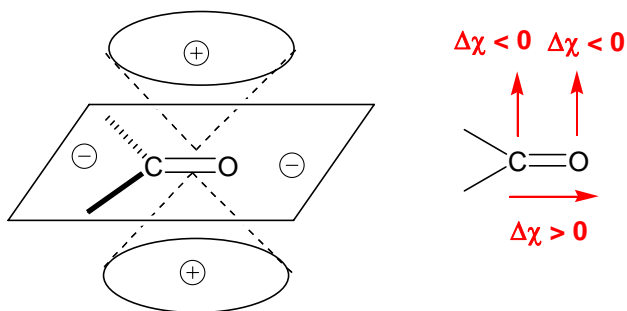
(c) C-C



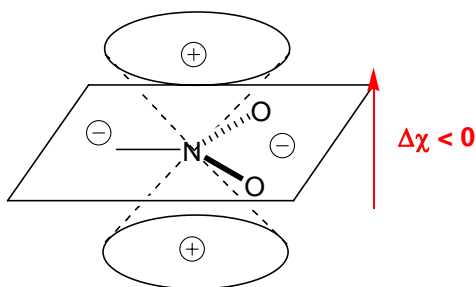
(d) C=C



(e) C=O



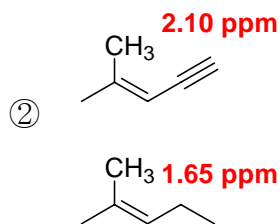
(f) NO₂



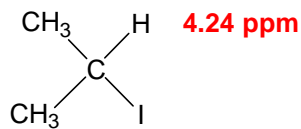
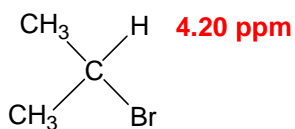
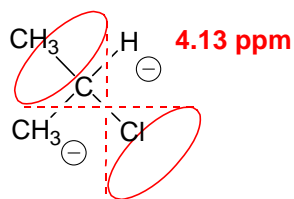
Examples

(a) C≡X

① CH₃-C≡C-H 1.80 ppm (quintet)



(b) C-X

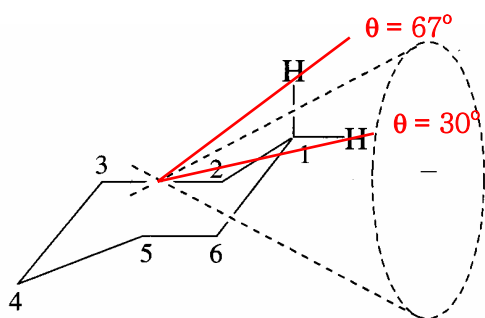


$|\Delta\chi|$ for C-X Cl < Br < I

c.f.

①	CH ₃ Cl	CH ₃ Br	CH ₃ I
	3.05	2.68	2.16 ppm
②	CH ₃ CH ₂ Cl	CH ₃ CH ₂ Br	CH ₃ CH ₂ I
	3.57	3.36	3.20 ppm

(c) C-C

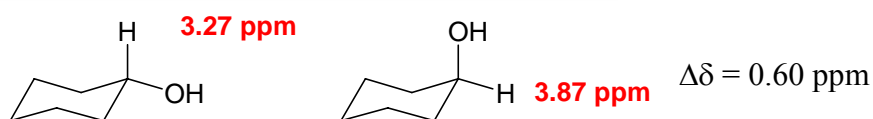


$$\theta_{ax} = 67^\circ$$
$$r_{ax} = 2.35 \text{ \AA}$$

$$\theta_{eq} = 30^\circ$$
$$r_{eq} = 2.80 \text{ \AA}$$

$$\delta_{Heq} - \delta_{Hax} \approx 0.4 \sim 0.6 \text{ ppm}$$

FIGURE 3.24 Deshielding of equatorial proton of a rigid six-membered ring.



(d) C=C

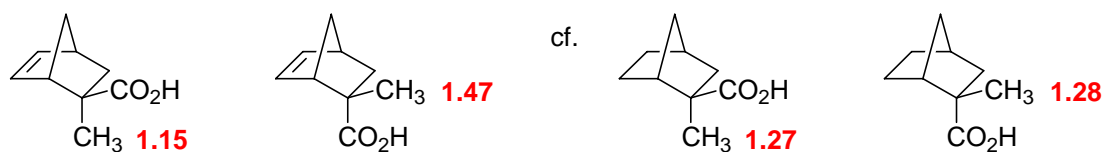
①



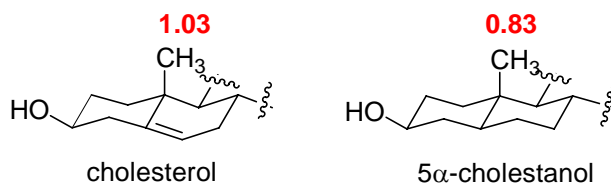
②



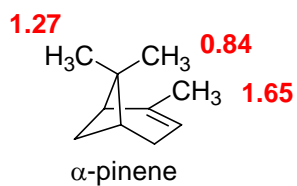
③



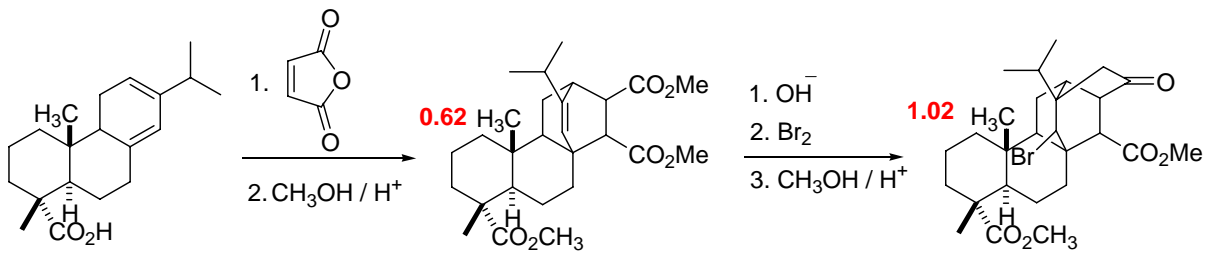
④



⑤



⑥

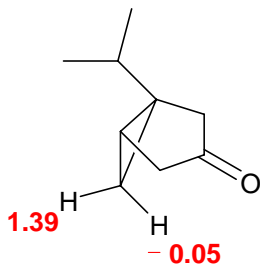


⑦

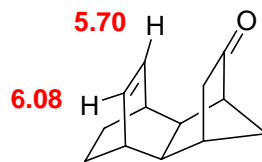


(e) C=O

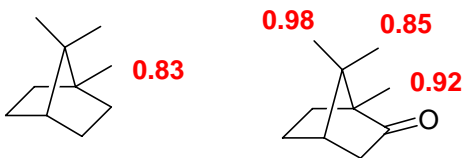
①



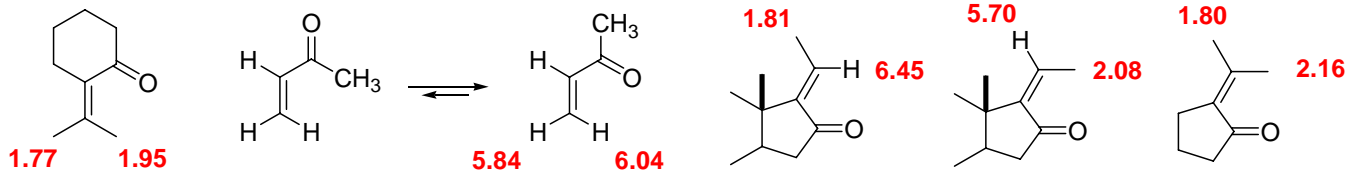
②



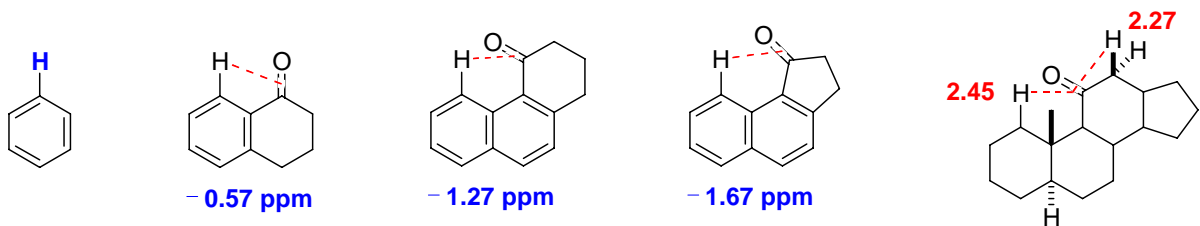
③



④



⑤ Deshielding

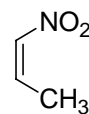
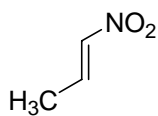


(f) -NO₂

①

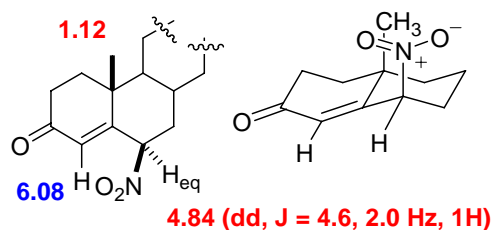
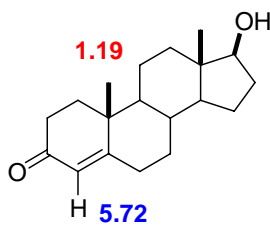
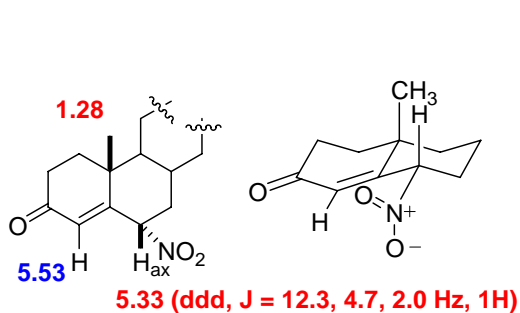


②

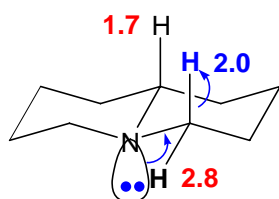


0.27 ppm deshielded
relative to the trans isomer

③

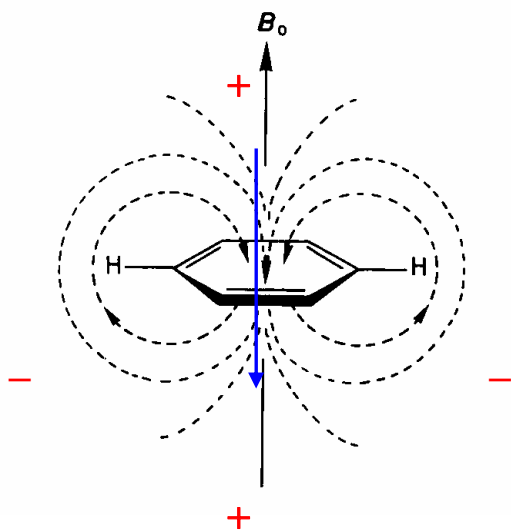


(g) "Quinolizidine" type



Axial hydrogens α to N are shielded by ~ 1 ppm relative to the equatorial hydrogens

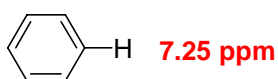
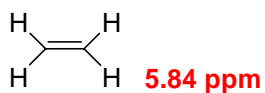
(h) Interatomic currents: Ring currents



$$\Delta\chi(\text{benzene}) = -96 \times 10^{-30} \text{ cm}^3 \cdot \text{esu}$$
$$\Delta\sigma = -H'/H_0 = \Delta\chi_z(1 - 3\cos^2\theta)/3R^3$$

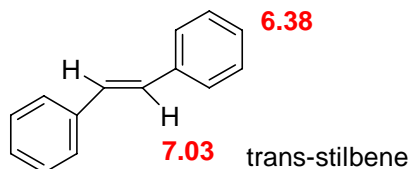
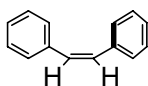
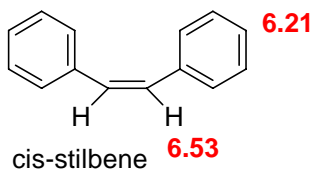
Magnetic field induced by ring currents in the benzene rings

Note



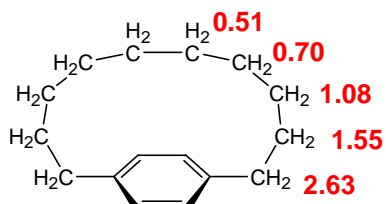
Examples

①



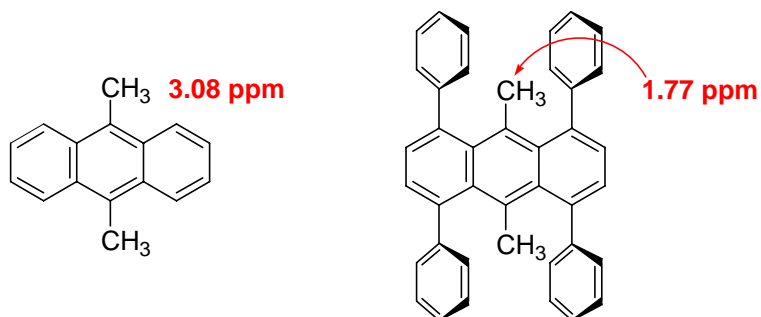
6.38

②



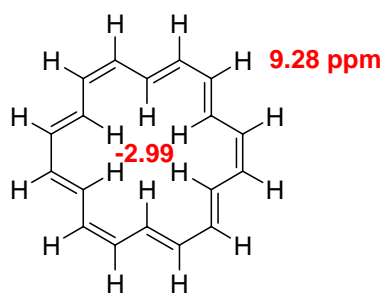
[10]-paracyclophane

③ *J. Am. Chem. Soc.* 1967, 89, 5458.

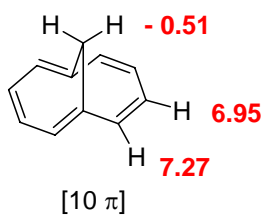


④ Aromatic $(4n+2)\pi$ system

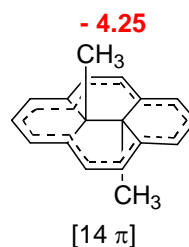
The shielding effect of the ring current is proportional to the area of the ring.



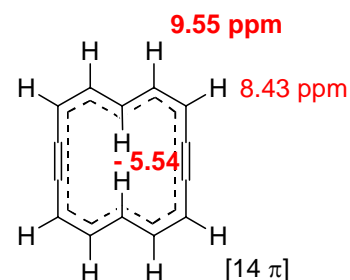
[18] annulene



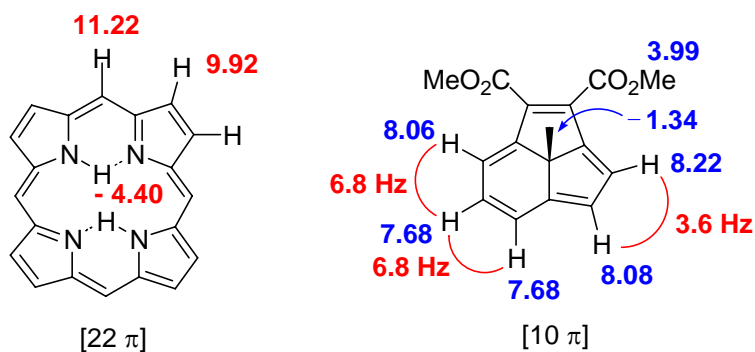
[10 π]



[14 π]



[14 π]



⑤ Doubly-bridged [16] annulene

Tetrahedron Lett. **1982**, 23, 1221; **1985**, 26, 3087; **1985**, 26, 3091.

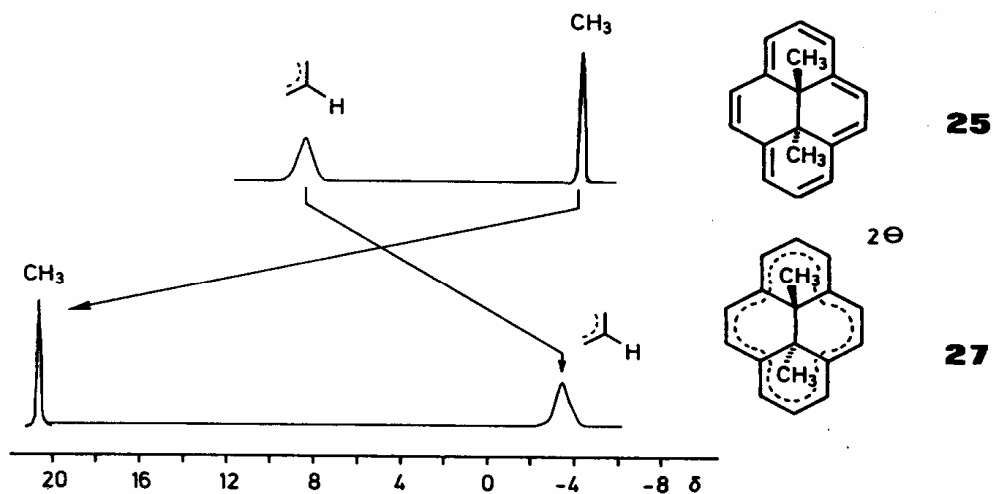
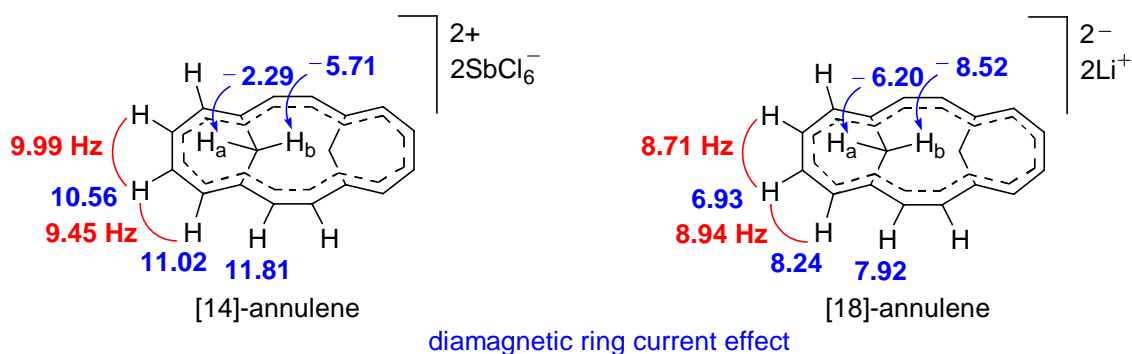
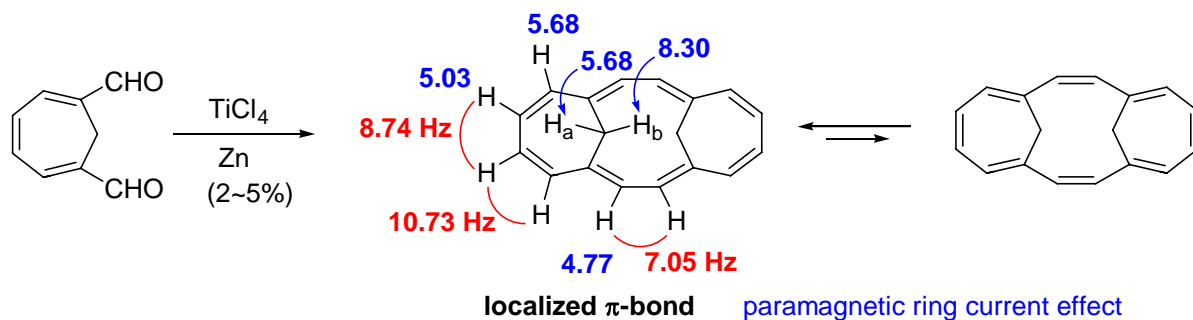
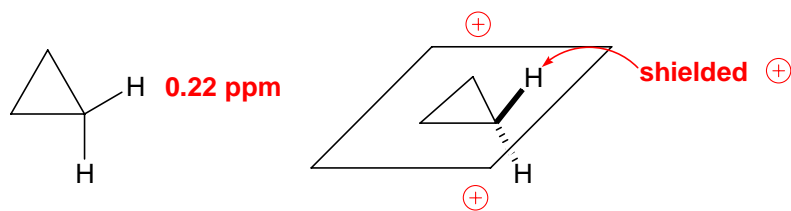


Figure 4.13 Schematic comparison of n.m.r. spectra of the annulenes **25** and **27** with 14 and 16 π-electrons, respectively

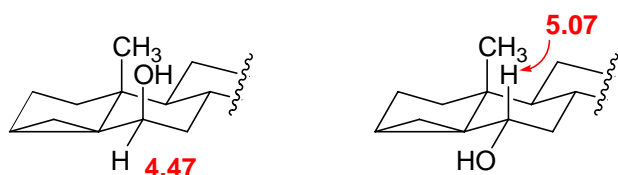
(i) Shielding effect by three-membered rings

(1) Cyclopropane ring



Examples

①



②

0.30 ppm up-field shifted



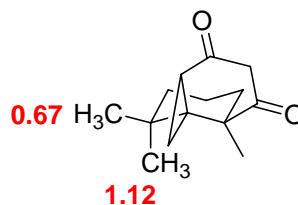
③



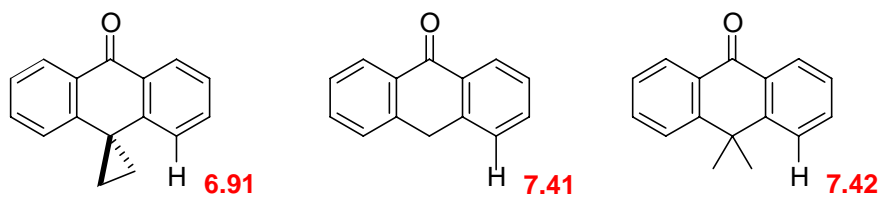
④



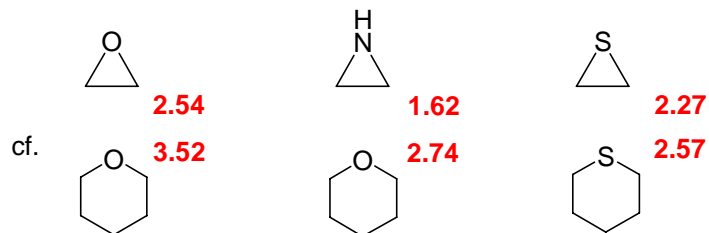
⑤

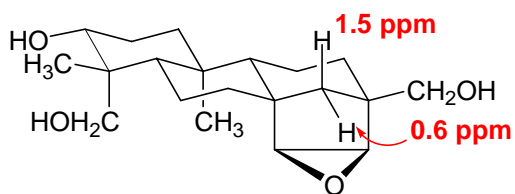


⑥



(2) Other three-membered rings





5.2 Proton Chemical Shifts in Aromatic Molecules Substituted Benzenes

Spectroscopy for Organic Molecules

Myong Ji Univ., Dept. of Chem.

Proton chemical shifts in aromatic molecules

Substituted benzenes

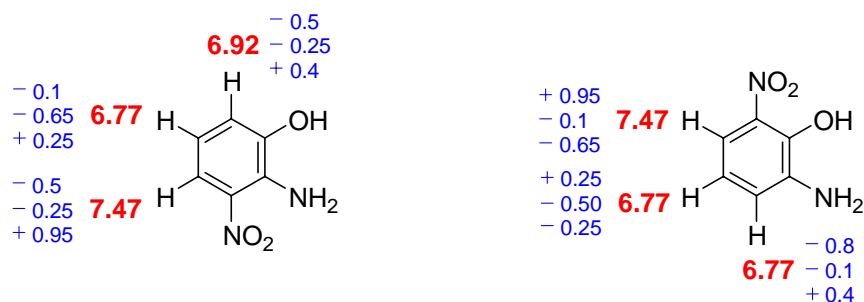
$$\delta_{\text{Ar-H}} = 7.27 + \sum P_i$$

Table for the P_i values

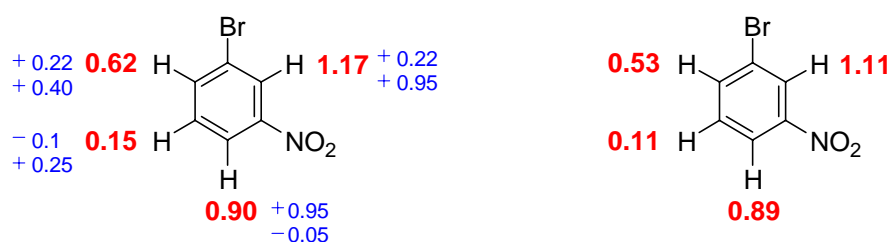
subst.	P_i^o	P_i^m	P_i^p	subst.	P_i^o	P_i^m	P_i^p
NHMe	-0.9	-0.2	-0.7	Br	0.22	-0.1	-0.05
NH ₂	-0.8	-0.25	-0.65	C (sp)	0.2	-0.05	-0.05
NMe ₂	-0.65	-0.2	-0.65	Ph	0.2	0.05	-0.05
OH	-0.5	-0.1	-0.5	CN	0.25	0.2	0.3
OMe	-0.5	-0.1	-0.45	I	0.4	-0.25	0
OR	-0.35	-0.05	-0.3	NHCOR	0.4	-0.2	-0.3
F	-0.3	0	-0.25	N ⁺ H ₃	0.4	0.2	0.2
Me	-0.15	-0.1	-0.15	COAr	0.45	0.1	0.2
CMe ₃	-0.1	0	-0.25	CHO	0.55	0.2	0.3
OCOPh	-0.1	0.05	-0.1	COR	0.6	0.1	0.2
SH	-0.05	-0.1	-0.2	COOR	0.7	0.1	0.2
Cl	0	-0.05	-0.1	CONH ₂	0.7	0.2	0.25
SR	0.1	-0.1	-0.2	COCl	0.8	0.2	0.35
C (sp ²)	0.15	0	-0.15	COOAr	0.9	0.15	0.25
OCOR	0.2	-0.1	-0.2	NO ₂	0.95	0.25	0.4

Examples

①



② $\Delta\delta$



Calcd values based on the equation

Observed values

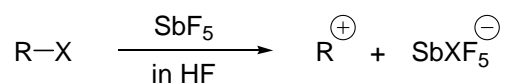
Heteroaromatics

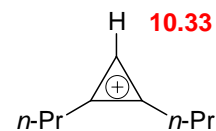
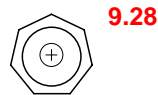
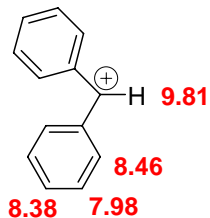
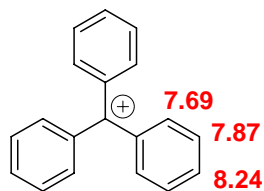
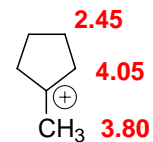
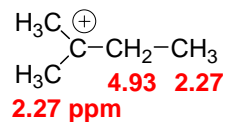
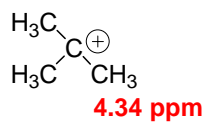
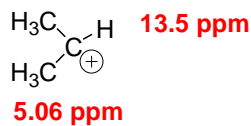
1. α -Protons are strongly up-field shifted by the heteroatom.
2. Asymmetric electron distribution: electron density is higher near the heteroatom, which lowers the aromaticity

		δ ppm (relative to benzene)	ρ_{exp}
	H-2	-1.31	0.91
	H-3	+0.16	1.01
	H-4	-0.26	0.98

5.3 Carbonium Ions, Carbanions and Related Systems

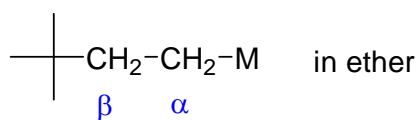
Carbonium ions





Carbanions

①

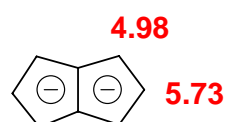
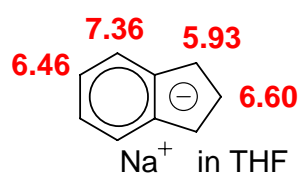
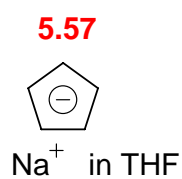


Chemical shift (δppm)

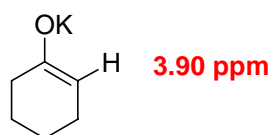
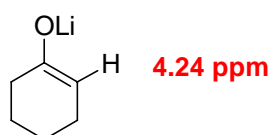
M	Li	Mg	Zn	Al	Hg
α	-1.08	-0.68	0.15	-0.20	1.01
β	1.35	1.39	1.47	1.25	1.58
e.n. of M	1.0	1.2	1.5	1.5	1.9
	Ionic			Covalency	

e.n.: electronegativity

②



③



more covalent character

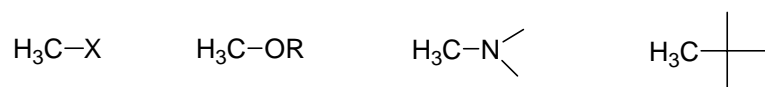
Table 4.1 Proton resonances in carbocations and carbanions

$\begin{array}{c} \text{H}_3\text{C} \\ \\ \text{C}^{\oplus} - \text{H} \\ \\ \text{H}_3\text{C} \end{array}$	$\begin{array}{c} \text{CH}_3 \\ \\ \text{H}_3\text{C} - \text{C}^{\ominus} \\ \\ \text{CH}_3 \end{array}$	$\begin{array}{c} \text{H} \quad \delta \ 10.3 \\ \diagup \quad \diagdown \\ \text{C}_3\text{H}_7 \quad \text{C}^{\oplus} \\ \diagdown \quad \diagup \\ \text{CH}_2 - \text{CH}_2 - \text{CH}_3 \end{array}$
$\delta \ 5.06 \ 13.50$	$\delta \ 4.35$	$\delta \ 3.15 \ 1.88 \ 1.01$
$[\text{CH}_2 \text{---} \text{CH} \text{---} \text{CH}_2]^{\oplus}$	$\begin{array}{c} \text{H}_3\text{C} \quad \text{C}^{\oplus} \quad \text{CH}_3 \\ \quad \\ \text{CH}_2 \quad \text{CH}_2 \\ \quad \\ \text{H}_3\text{C} \quad \text{CH}_3 \end{array}$	$\text{CH}_3\text{Li} \quad \text{CH}_3 - \text{CH}_2\text{Li}$
$\delta \ 8.97 \ 9.64 \ 8.97$	$\delta \ 1.21$	$\delta \ -1.3 \ 1.33 \ -0.99$
$[\text{CH}_2 \text{---} \text{CH} \text{---} \text{CH}_2]^{\ominus}$	$\begin{array}{c} \text{H}_3\text{C} \quad \text{C}^{\oplus} \quad \text{CH}_3 \\ \quad \\ \text{CH}_2 \quad \text{CH}_2 \\ \quad \\ \text{H}_3\text{C} \quad \text{CH}_3 \end{array}$	$(\text{CH}_3)_2\text{Mg} \quad (\text{CH}_3 - \text{CH}_2)_2\text{Mg}$
$\delta \ 2.46 \ 6.28 \ 2.46$	$\delta \ 3.07$	$\delta \ -1.3 \ 1.26 \ -0.64$
	$\delta \ 3.33$	$(\text{CH}_3 - \text{CH}_2 - \text{CH}_2)_2\text{Mg}$
	$\delta \ 8.02$	$\delta \ 0.90 \ 1.50 \ -0.57$
$\text{C}_6\text{H}_5 - \text{CH}_2\text{Li}$	$\text{C}_6\text{H}_5 - \text{C}^{\oplus}(\text{CH}_3)_2$	$\text{C}_6\text{H}_5 - \text{N}^{\oplus}(\text{CH}_3)_3$
$\delta_o \ 6.09$	8.80	7.98
$\delta_m \ 6.30$	7.97	7.66
$\delta_p \ 5.50$	8.45	7.60

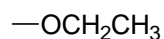
6. Non-first-order Spin Systems

6-1. Nomenclature of the spin system

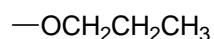
A_3 (singlet)



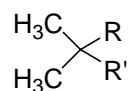
A_2X_3 (quartet)(triplet)



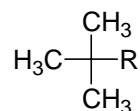
$A_2M_2X_3$ or $A_2X_2Y_3$ (triplet)(sextet)(triplet)



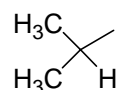
A_6 (singlet) or A_3B_3 (2 singlet)



A_9 (singlet)



AX_6 or AX_3Y_3 (doublet or 2 doublet for Me)



For first-order spectra

(i) Chemical shift separation \gg the coupling constant

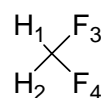
(ii) Magnetically equivalent nuclei

The Pascal Triangle for $I = 1/2$

Magnetically equivalent nuclei vs. chemically equivalent nuclei

Magnetically equivalent nuclei \rightleftharpoons Chemically equivalent nuclei

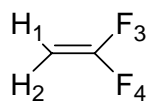
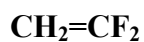
CH_2F_2



$$J_{1,3} = J_{2,3}$$

$$J_{1,4} = J_{2,4}$$

A_2X_2 (magnetically equivalent)



$J_{1,3} \neq J_{2,3}$

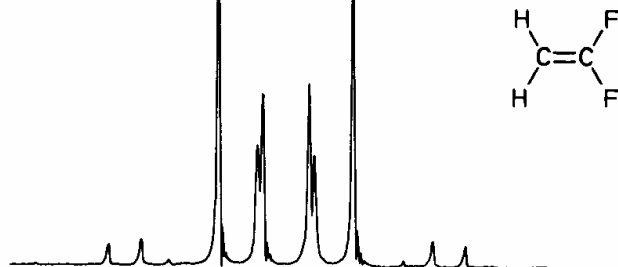
$J_{1,4} \neq J_{2,4}$

AA'XX' (magnetically nonequivalent)

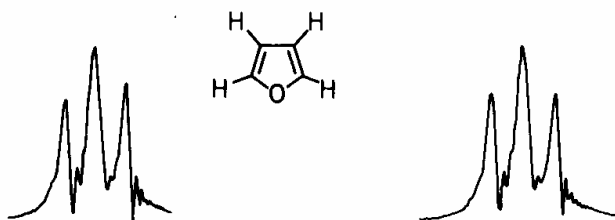
a



b

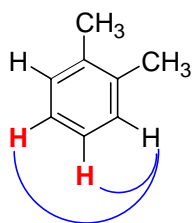


c

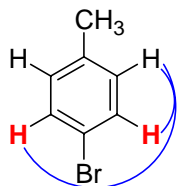


$B_0 \longrightarrow$

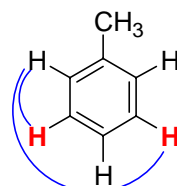
Figure 2.21 Proton magnetic resonance spectrum of (a) difluoromethane, (b) 1,1-difluoroethylene (after Ref. 2), and (c) furan



AA'BB'



AA'XX'



AA'BB'C

more than 100 lines

6.2 Two-Spin Systems

$\Delta\nu(\text{Ha,Hb}) / J(\text{Ha,Hb})$

AX \longrightarrow AB \longrightarrow AA' \longrightarrow A₂

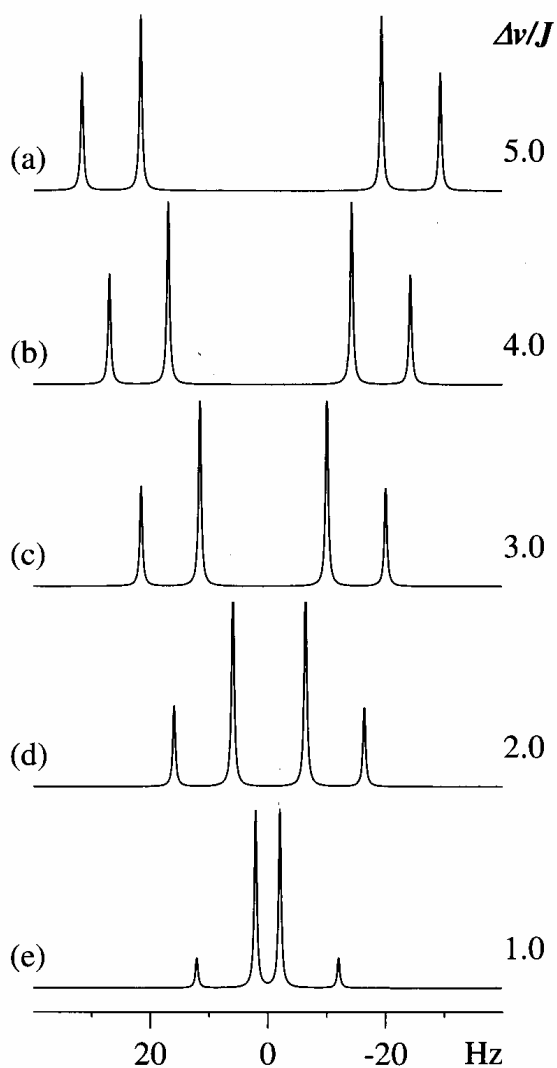


FIGURE 3.28 A two-proton system, spin coupling with a decreasing difference in chemical shifts and a large J value (10 Hz); the difference between AB and AX notation is explained in the text.

► The AB System

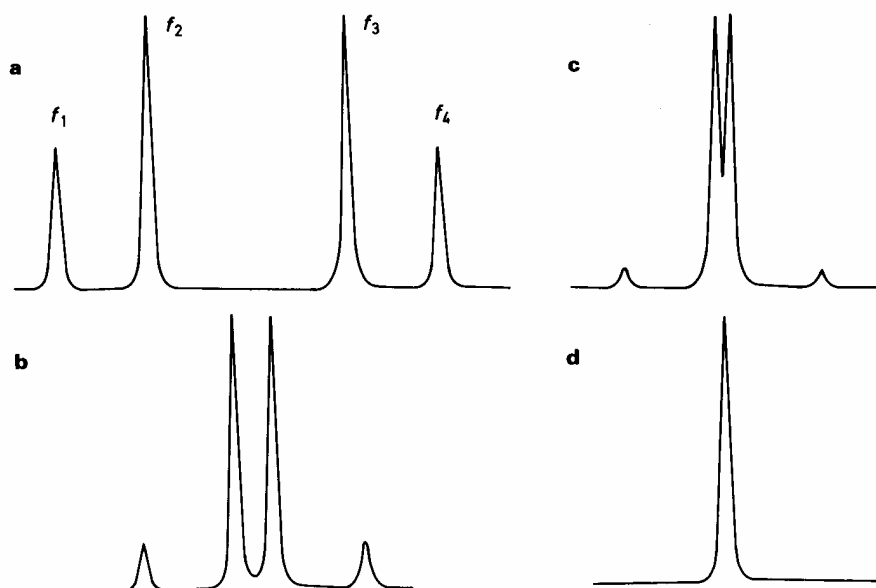
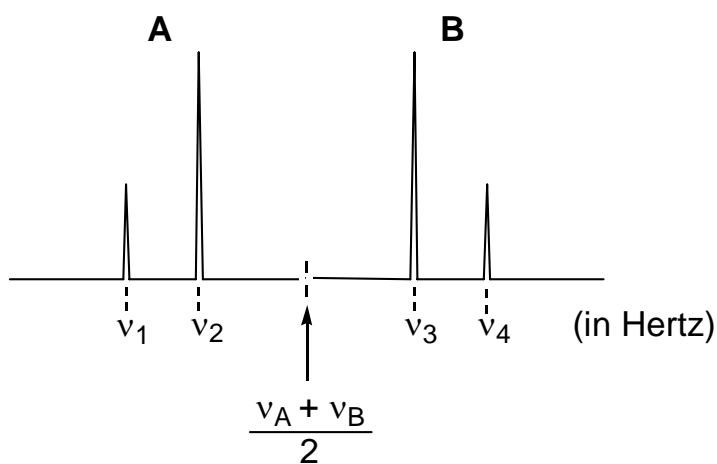


Figure 5.5 Dependence of the AB system on the ratio $J/v_0\delta$; spectra illustrated are for values of $J/v_0\delta$ of (a) 1:3, (b) 1:1, (c) 5:3, and (d) 5:1.



a. Symmetrical around $(\nu_A + \nu_B)/2$

$$\nu_1 - \nu_2 = \nu_3 - \nu_4$$

$$I_1 : I_2 = I_4 : I_3$$

b. $J_{AB} = \nu_1 - \nu_2 = \nu_3 - \nu_4$

(or get average)

c. $\nu_A - \nu_B = \{(\nu_1 - \nu_4)(\nu_2 - \nu_3)\}^{1/2}$

d. $I_1 / I_2 = I_4 / I_3 = (\nu_2 - \nu_3) / (\nu_1 - \nu_4)$

$$\nu_1 - \nu_2 = \nu_3 - \nu_4 = J_{AB}$$

Calculation of the chemical shift in AB system

Suppose $(\nu_A + \nu_B)/2 = X$, $\nu_A - \nu_B = \{(\nu_1 - \nu_4)(\nu_2 - \nu_3)\}^{1/2} = Y$

Then

$$\nu_A + \nu_B = 2X,$$

$$\nu_A - \nu_B = Y$$

Solve the two equations for ν_A and ν_B

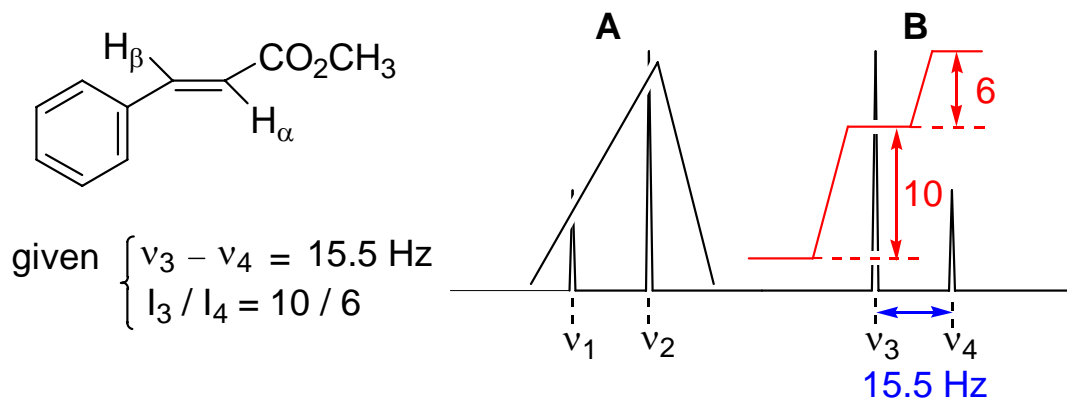
$$\nu_A = (2X + Y)/2 \quad \nu_B = (2X - Y)/2$$

$$\therefore \nu_A = (\nu_A + \nu_B)/2 + \{(\nu_1 - \nu_4)(\nu_2 - \nu_3)\}^{1/2}/2$$

$$\nu_B = (\nu_A + \nu_B)/2 - \{(\nu_1 - \nu_4)(\nu_2 - \nu_3)\}^{1/2}/2$$

※ Even if one of the two protons is hidden, exact parameter can be determined.

e.g.



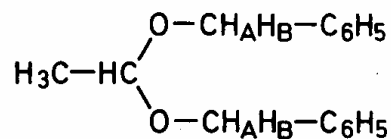
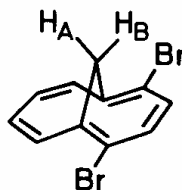
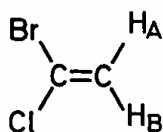
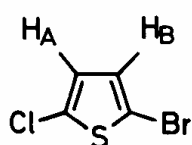
Suppose $(\nu_2 - \nu_3) = X$

Then $(\nu_2 - \nu_3) / (\nu_1 - \nu_4) = X / (X + 2J) = I_1 / I_2 = I_4 / I_3 = 6 / 10$

Since $J = 15.5 \text{ Hz}$,

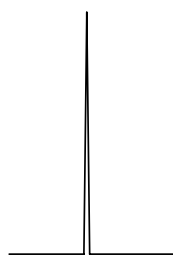
therefore $X = 3J = 46.5 \text{ Hz}$

Some examples of the AB system



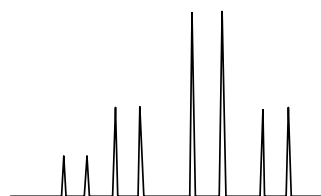
6.3 Three-Spin Systems

(1)

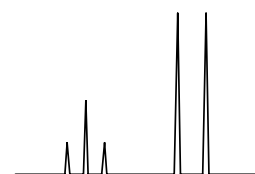
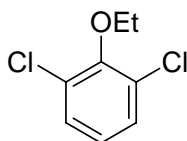


A_3

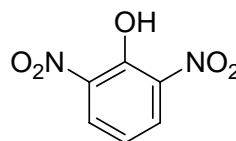
$$\frac{\Delta\nu(A,B)}{J(A,B)} \longrightarrow 0$$



AB_2

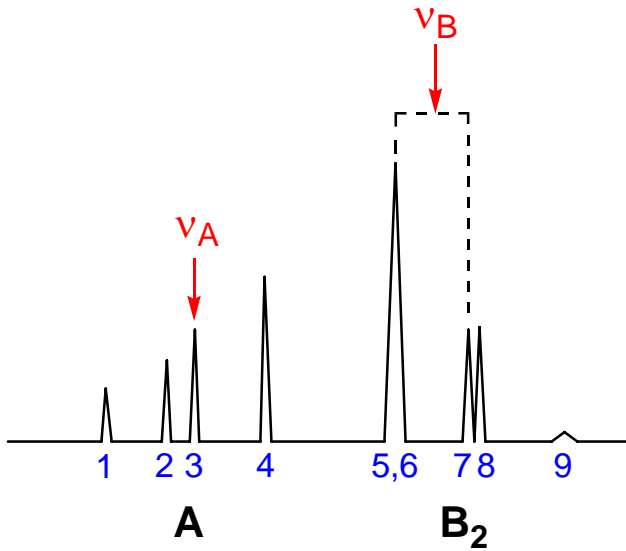
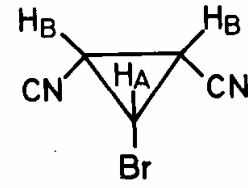
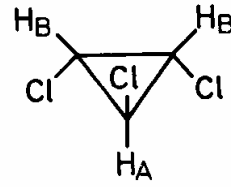
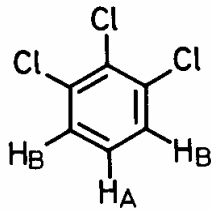
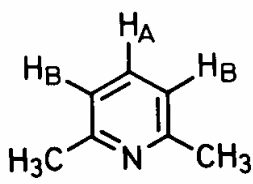


$A \quad X_2$



$$\frac{\Delta\nu(A,B)}{J(A,B)} \longrightarrow \infty$$

AB₂ System



1. $\nu_3 = \nu_A$

2. $(\nu_5 + \nu_7) / 2 = \nu_B$

3. ν_9 : combination band

$$2(\nu_B - \nu_A) = (\nu_9 - \nu_3) - (\nu_3 - \nu_2)$$

4.

$$(\nu_4 - \nu_3) + (\nu_8 - \nu_3) = (\nu_B - \nu_A) + 3J_{AB}/2$$

e.g.

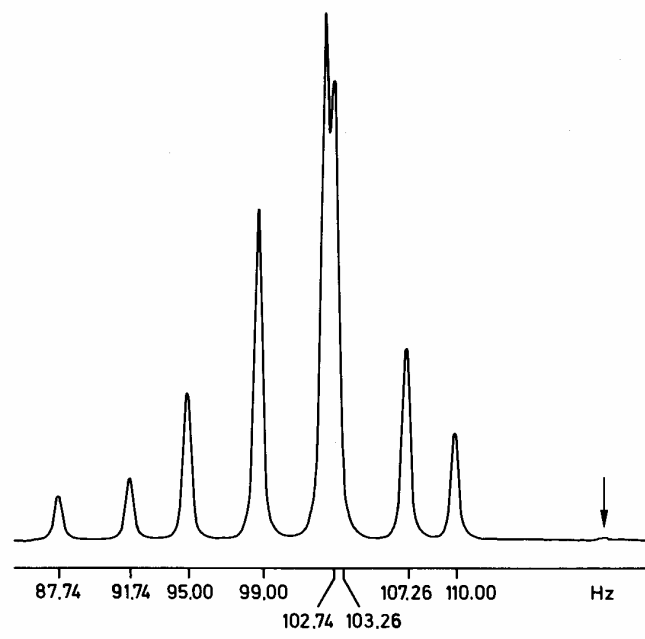
$$\nu_3 = 0, \nu_4 = 6.6 \text{ Hz}, \nu_5 = 19.3 \text{ Hz}, \nu_7 = 25.6 \text{ Hz}, \nu_8 = 27.7 \text{ Hz}$$

Using the equation 4, $6.6 + 27.7 = (\nu_B - \nu_A) + 3J_{AB}/2$

According to the equations 1 and 2, $(\nu_B - \nu_A) = (19.3 + 25.6) / 2 = 22.5$

Therefore $J_{AB} = 7.86 \text{ Hz}$

Exercise 5.10 Analyse the AB₂ spectrum below and determine the parameters ν_A , ν_B , and J_{AB} .



(2) **ABX System:** normally 12 peaks and maximum 15 peaks

$$|\nu_X - \nu_A| \gg J_{AX}; \quad |\nu_X - \nu_B| \gg J_{BX}$$

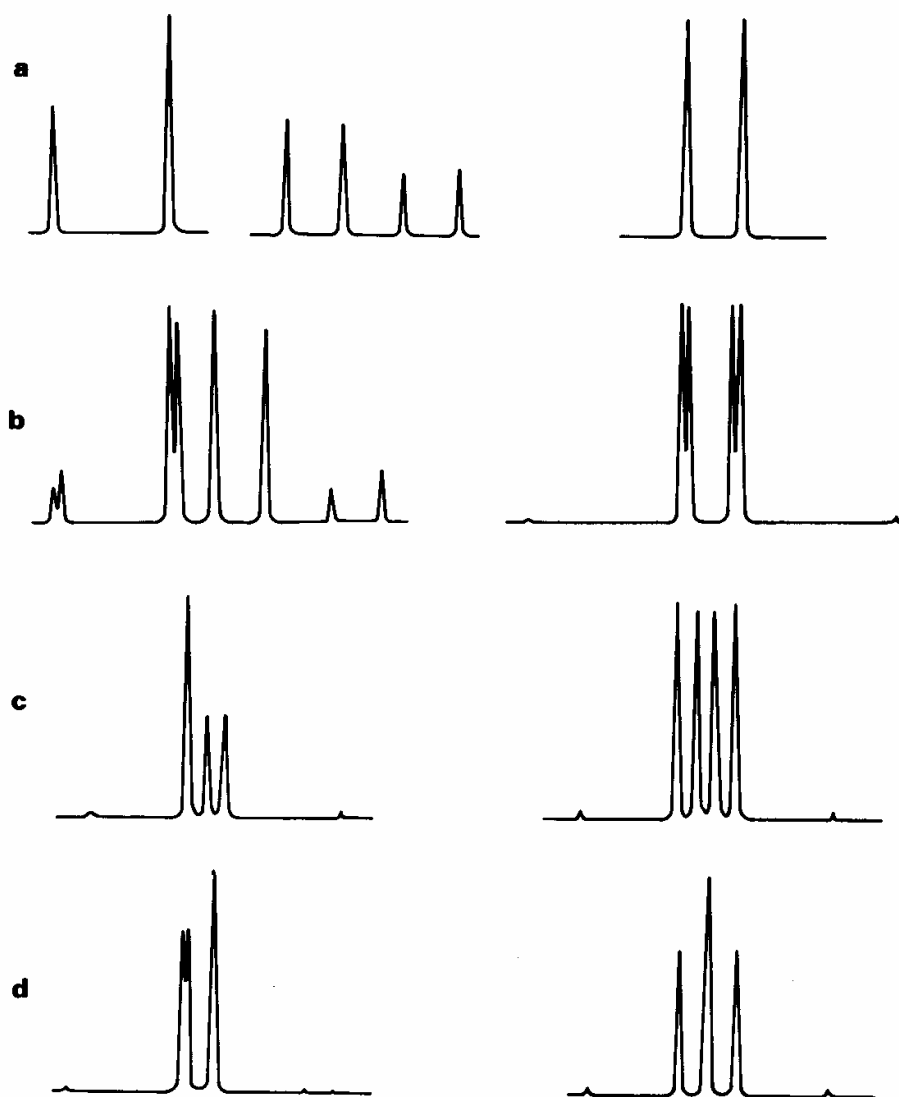
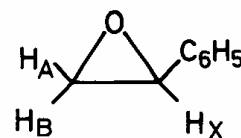
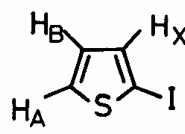
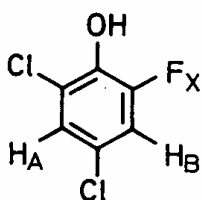
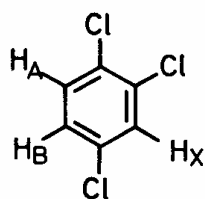
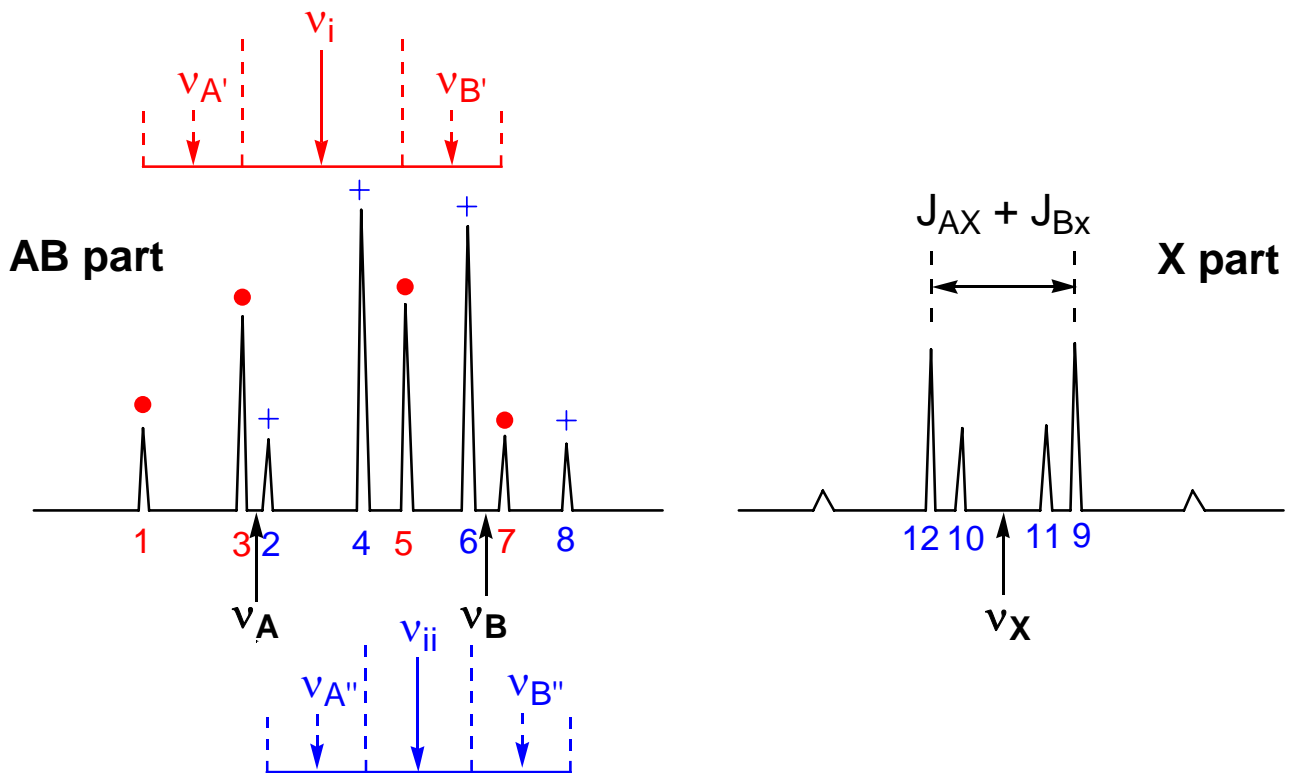


Figure 5.17 Dependence of the ABX system on the parameter $\nu_A - \nu_B$: left, the AB portion; right, the X portion. The following parameters apply in all examples: $J_{AB} = 15.7$ Hz; $J_{AX} = 0$ Hz; and $J_{BX} = 7.7$ Hz. The relative chemical shifts $\nu_0\delta$ (AB) amount to (a) 56.7 Hz, (b) 18.7 Hz, (c) 5.0 Hz, and (d) -0.6 Hz. Experimental data from 2-furfuryl-(2)-acrolein form the basis for the calculated spectra (after Ref. 3)

Examples of ABX system



Peaks Analysis



1. $\mathbf{J_{AB}} = v_3 - v_1 = v_4 - v_2 = v_7 - v_5 = v_8 - v_6$
2. $v_{12} - v_9 = \mathbf{J_{AX}} + \mathbf{J_{BX}}$
3. $v_i - v_{ii} = (\mathbf{J_{AX}} + \mathbf{J_{BX}}) / 2$
 v_i, v_{ii} : center of the two AB's
4. $\mathbf{v_A} = (v_{A'} + v_{A''}) / 2$, $\mathbf{v_B} = (v_{B'} + v_{B''}) / 2$

Analysis of ABX assuming two AB sub-spectra

v_i, v_{ii} : center of the two AB's

$$\Delta_i = v_{A'} - v_{B'}, \quad \Delta_{ii} = v_{A''} - v_{B''}$$

$$J_{AX} \cdot J_{BX} > 0$$

$$v_A = (v_i + v_{ii})/2 + (\Delta_i + \Delta_{ii})/4$$

$$v_B = (v_i + v_{ii})/2 - (\Delta_i + \Delta_{ii})/4$$

$$J_{AB} = (v_i - v_{ii}) + (\Delta_i - \Delta_{ii})/2$$

$$J_{BX} = (v_i - v_{ii}) - (\Delta_i - \Delta_{ii})/2$$

$$J_{AX} \cdot J_{BX} < 0$$

$$v_A = (v_i + v_{ii})/2 + (\Delta_i - \Delta_{ii})/4$$

$$v_B = (v_i + v_{ii})/2 - (\Delta_i - \Delta_{ii})/4$$

$$J_{AB} = (v_i - v_{ii}) + (\Delta_i + \Delta_{ii})/2$$

$$J_{BX} = (v_i - v_{ii}) - (\Delta_i + \Delta_{ii})/2$$

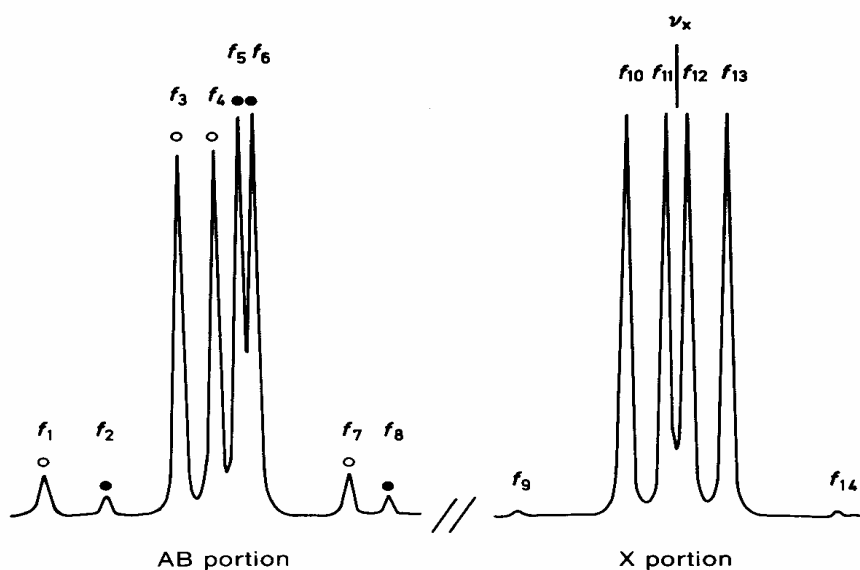


Figure 5.10 The ABX system with the parameters $\nu_0\delta$ (AB) = 5.0 Hz, J_{AB} = 8 Hz, J_{AX} = 4.2 Hz and J_{BX} = 1.8 Hz. The ab subspectra in the AB portion are identified by the open and closed circles. The parameters used are those of 2-chloro-3-aminopyridine (after Ref. 1)

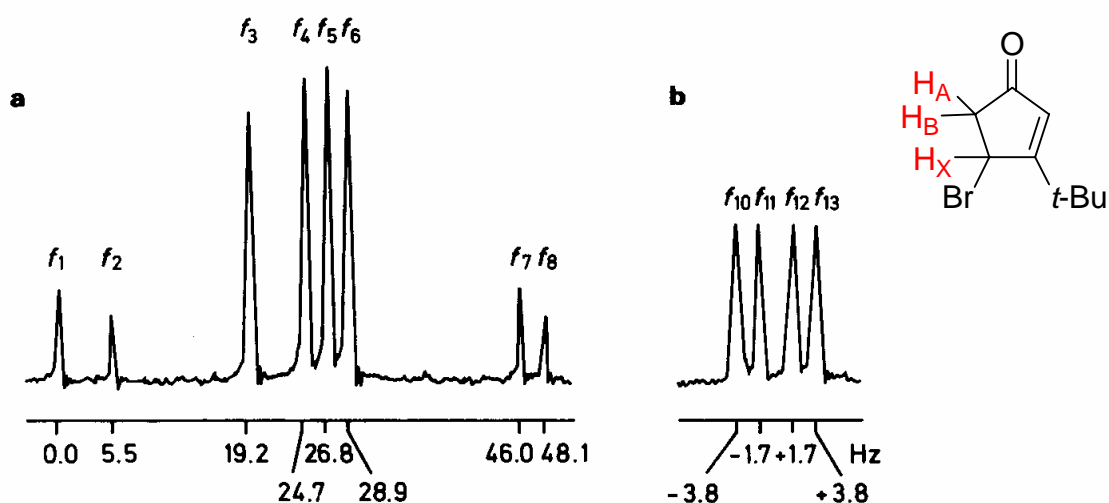


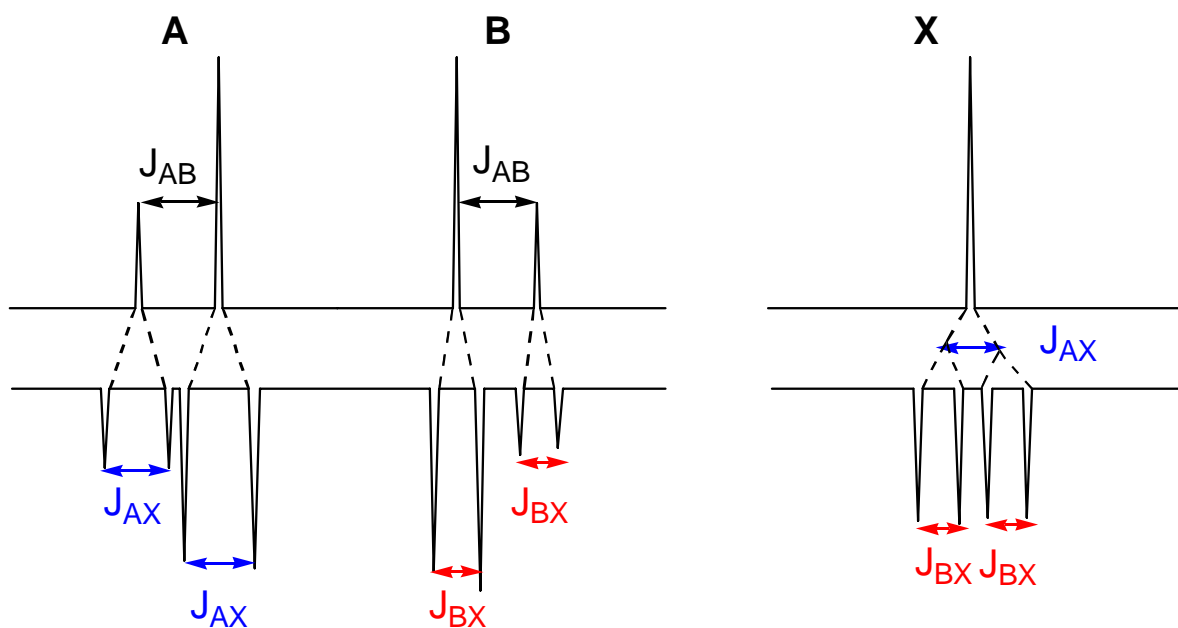
Figure 5.11 The ABX spectrum of 4-bromo-3-t-butylcyclopentene-2-one (**91**) (after Ref. 2): (a) AB portion, relative line frequencies in Hz; (b) X portion (in this case this lies at lower field); 60 MHz

In ABX system

If $(\nu_A - \nu_B)$ gets large then it becomes AMX system.

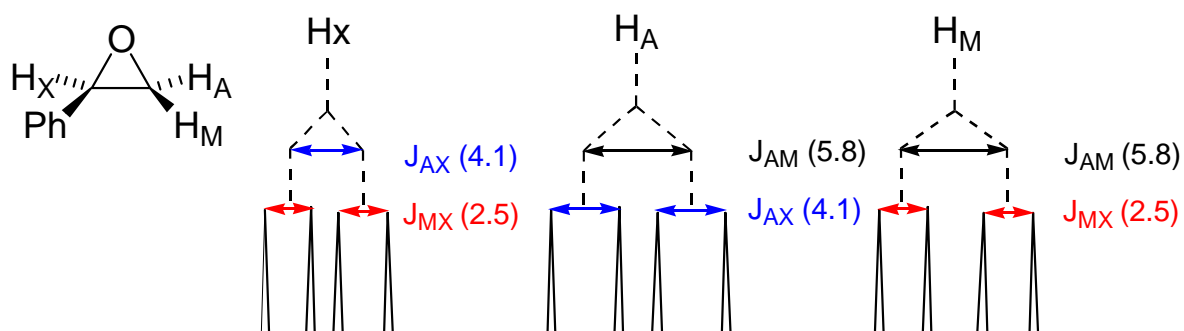
If ν_X comes close to ν_A, ν_B then it becomes ABC system.

One can analyze **ABX** system as **AMX** system (first-order system)

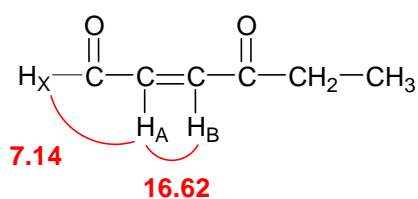


			First-order analysis J	Observed J
	(a) $J_{AX} \cdot J_{BX} > 0$	J_{AB}	7.35 Hz	7.35 Hz
		J_{AX}	4.68 Hz	5.0 Hz
		J_{BX}	1.62 Hz	1.3 Hz
	(b) $J_{AX} \cdot J_{BX} < 0$	J_{AB}	7.35 Hz	7.35 Hz
		J_{AX}	4.45 Hz	5.0 Hz
		J_{BX}	0.75 Hz	-1.3 Hz

AMX system

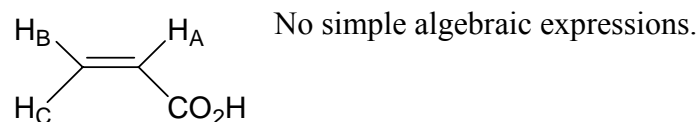


Virtual coupling

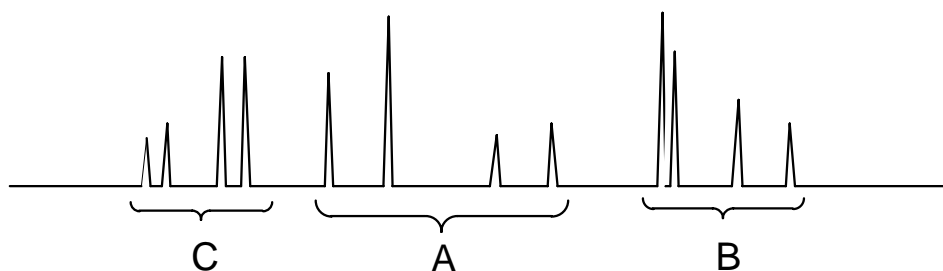
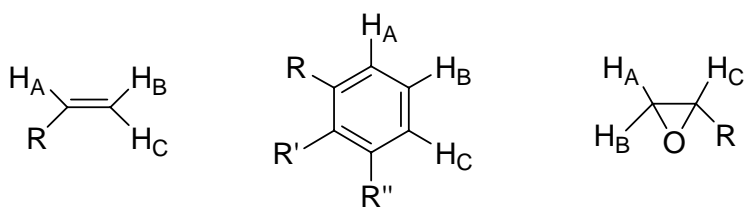


Even though H_X is coupled only to H_A , H_X consists of more than two lines (four lines)

(3) ABC System: Maximum 15 lines

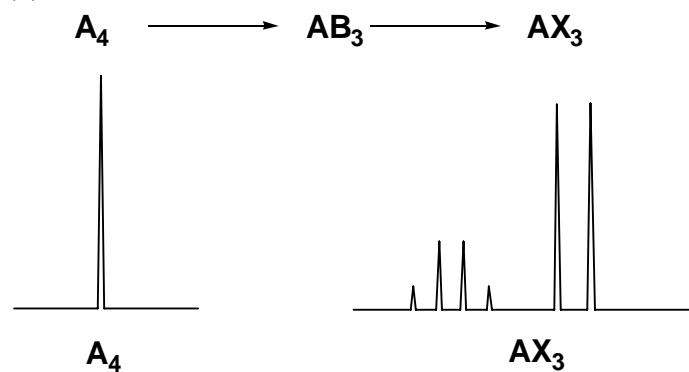


Examples

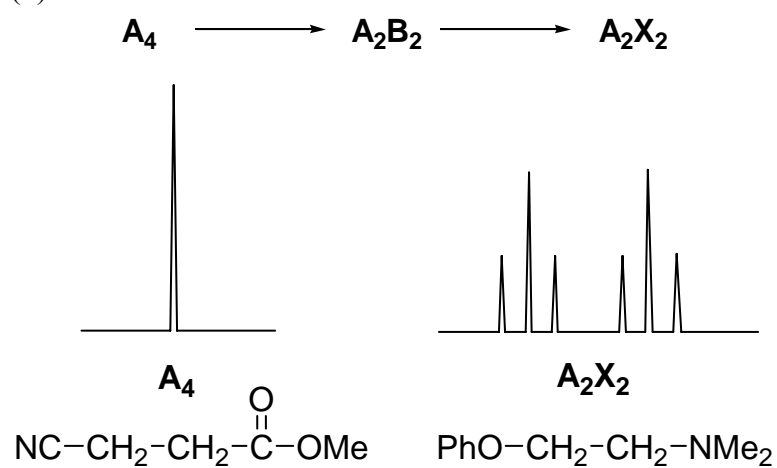


6.4 Four-Spin Systems

(1)



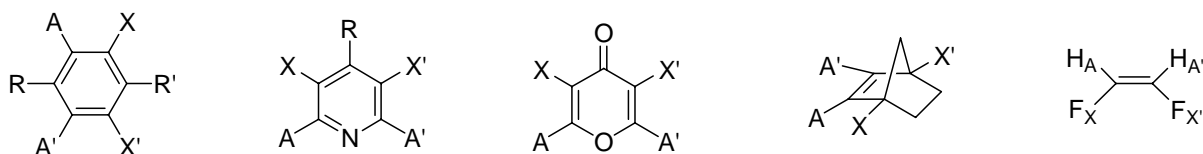
(2)



(3) **AA'XX'**: 24 lines

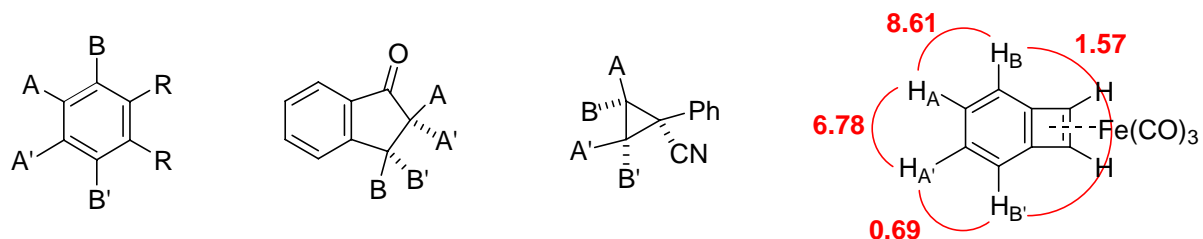
Normally 20 lines are observed

AA': Chemically equivalent but magnetically nonequivalent



(4) **AA'BB'**

If $\Delta\nu_{AX}$ becomes small, AA'XX' becomes AA'BB'. 24 lines are observed.

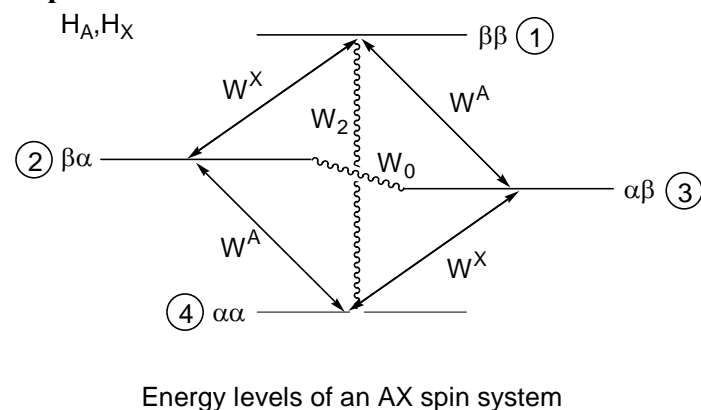


7. Nuclear Overhauser Effect (NOE)

Change in NMR intensity via change in Boltzmann distribution of a nuclear spin by a **dipolar mechanism upon saturation of a second interacting nuclear spin.**

Dipolar mechanism maintains the relaxation (T_1), thereby increasing ground state population
 → increased intensity.

Explanation



W^A : transition probability of spin A
 W^X : transition probability of spin X
 W_2 : transition probability between ① and ④ (double quantum jump) or relaxation – important when T_1^{DD} is important.
 W_0 : transition probability between ② and ③ (zero quantum jump) or relaxation.

Irradiation of X will saturate the transition ②→① and ④→③.

Therefore $P_1 = P_2, P_3 = P_4$ (P: population of each energy level).

Assuming that

Before irradiation, $P_2 \approx P_3 = C, P_2 - P_1 = P_4 - P_3 = \Delta$

Before irradiation

$$P_1 = C - \Delta$$

$$P_2 = C$$

$$P_3 = C$$

$$P_4 = C + \Delta$$

$$\therefore P_4 - P_1 = 2\Delta$$

After irradiation

$$P_1 = C - \Delta/2$$

$$P_2 = C - \Delta/2$$

$$P_3 = C + \Delta/2$$

$$P_4 = C + \Delta/2$$

$$\therefore P_4 - P_1 = \Delta$$

Now, W_2 process increases P_4 and decrease P_1 , thereby restoring the population difference to its equilibrium value, which enhances transition of A (increased intensity of nuclei A).

W_2 is very effective when T_1^{DD} (dipole-dipole) predominates.

There is a fractional enhancement of the A signal.

$$f = \frac{W_2 - W_0}{2W^A + W_2 + W_0} \left(\frac{\gamma_X}{\gamma_A} \right)$$

maximum limit: $\left(\frac{\gamma_X}{\gamma_A} \right) / 2$

↖ saturated or irradiated nuclei
↗ observed nuclei

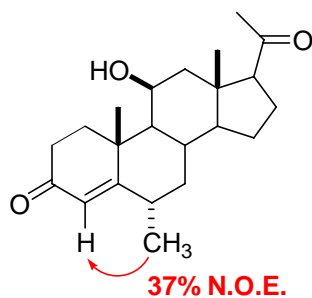
For proton, maximum N.O.E. = 50%; for carbon maximum N.O.E. = 200%

$$\text{N.O.E.} = 1/(\text{A} \cdot \tau_{\text{AB}}^6)$$

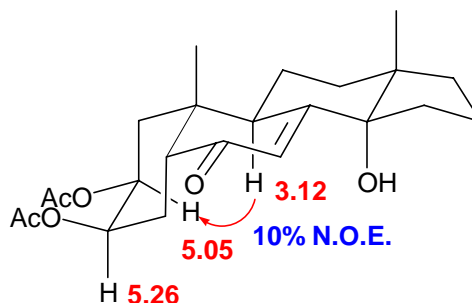
Effective N.O.E. can be obtained within the inter-atomic distance of **3Å**.

Examples

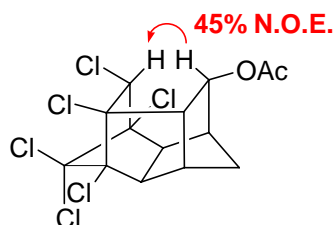
①



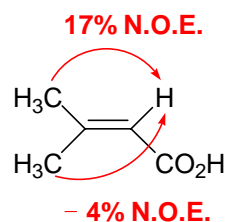
②



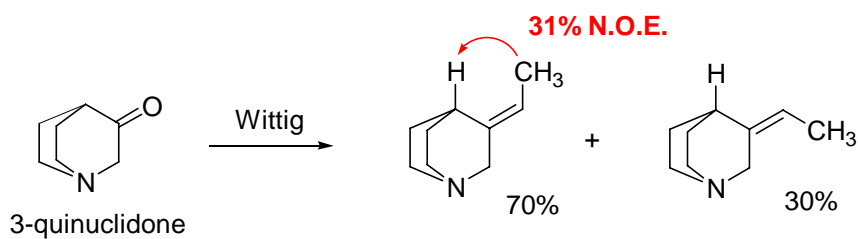
③



④

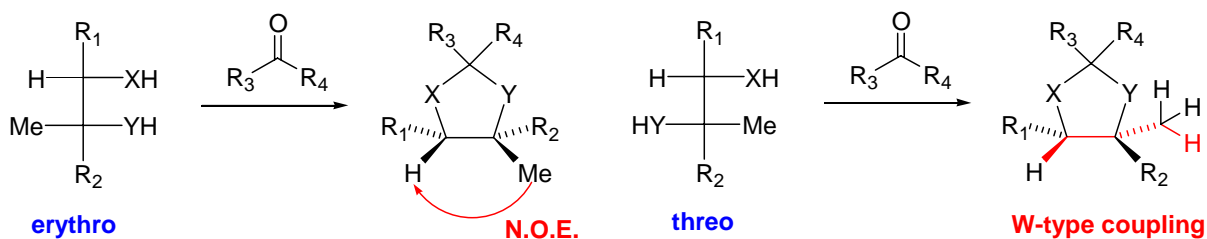


⑤

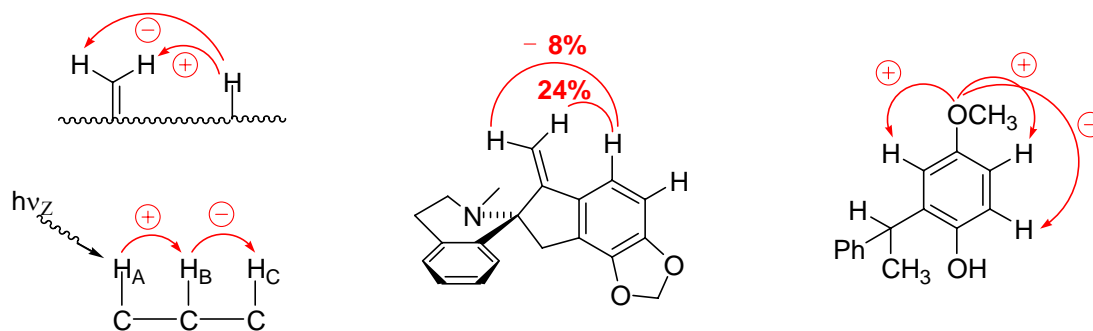


DMSO(d_6) is the best solvent for N.O.E. measurement. Solvent should be degassed, and preferably be sealed.

⑥ Threo & erythro isomers of α -glycols (*J. Am. Chem. Soc.* **1972**, *94*, 2865).



Negative N.O.E. in multi-spin system



Exercise 2.13. Figure 2.28 shows the 80 MHz ^1H n.m.r spectrum of 2,4-dinitrophenyl-2-pyridylsulphide. Assign the protons to the structural formula given and estimate the coupling constants.

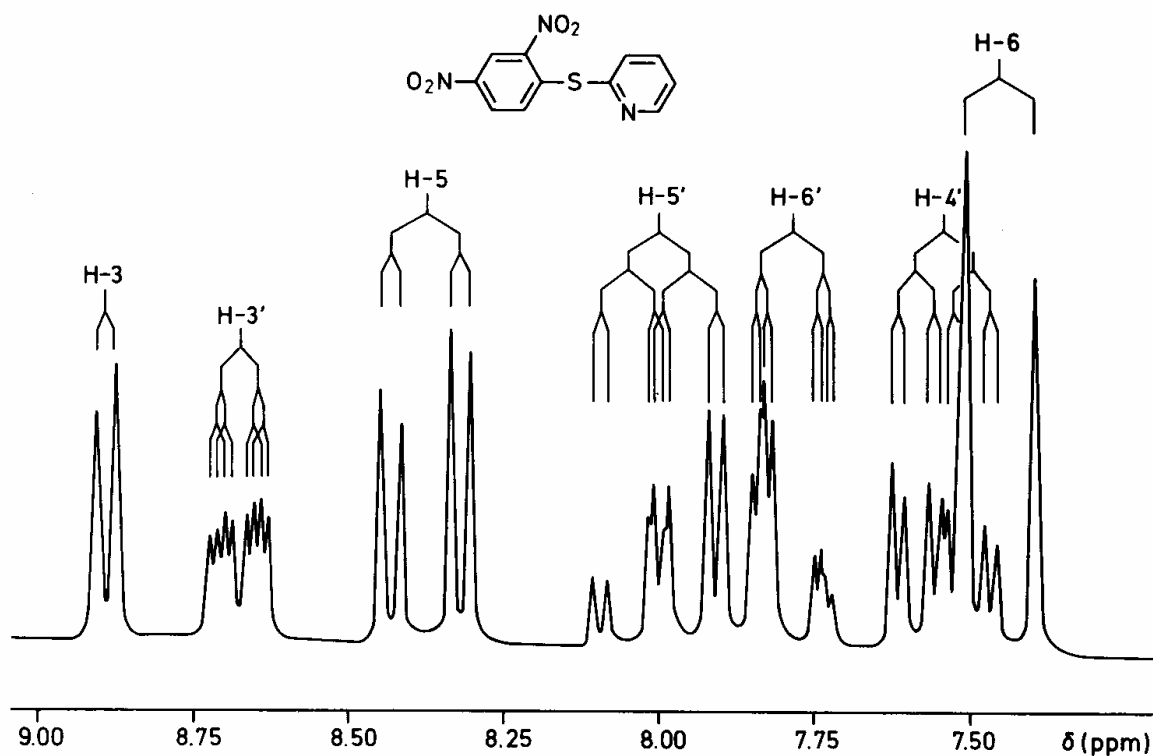


Figure 2.28 80 MHz ^1H n.m.r. spectrum of 2,4-dinitrophenyl-2-pyridylsulphide